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AN ANALYSIS OF THE PROPERTIES
OF TWO-DIMENSIONAL INCOMPRESSIBLE
FLUID FLOW IN THE MIXING CHAMBER
OF A CONSTANT AREA EJECTOR
MARTIN D. KIEFER

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AN ANALYSIS OF THE PROPERTIES OF TWO-DIMENSIONAL INCOMPRESSIBLE FLUID FLOW IN THE MIXING CHAMBER OF A CONSTANT AREA EJECTOR

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Martin D. Kiefer

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bу

Martin D. Kiefer

//
Lieutenant, United States Navy

Submitted in partial fulfillment of the requirements for the degree of

> MASTER OF SCIENCE IN · MECHANICAL ENGINEERING

United States Naval Postgraduate School Monterey, California

1963

AN ANALYSIS OF THE PROPERTIES

OF TWO-DIMENSIONAL INCOMPRESSIBLE FLUID FLOW

IN THE MIXING CHAMBER OF A CONSTANT AREA EJECTOR

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Martin D. Kiefer

This work is accepted as fulfilling the thesis requirements for the degree of MASTER OF SCIENCE

IN

MECHANICAL ENGINEERING

from the

United States Naval Postgraduate School

ABSTRACT

The properties of an incompressible fluid in the mixing chamber of a constant area cylindrical ejector are analyzed in a two-dimensional form. The flow field for velocity and temperature is assumed to be made up of regions in which uniform flow of the primary and secondary fluids exist, and which diminish with axial distance from the ejector entrance. The velocity and temperature distributions in the mixed region are assumed to have cosine shaped profiles. The compatible solutions are given an axial distribution by assuming a parabolic spread rate for the secondary fluid jet boundary.

Results are generated in the form of a non-dimensional velocity and pressure, a normalized temperature and a Momentum Factor, as functions of axial distance. Area ratios studied include 100:1, 9:1 and 2.25:1. Velocity ratios studied include 50:1, 10:1, 3:1 and 1.5:1. The Fortran programs employed to generate compatible solutions, titled EJECTMIX I and EJECTMIX II. are included.

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TABLE OF SYMBOLS AND ABBREVIATIONS

Fortran Symbol	Mathematical Symbol	Definition
ALPHA	·····································	numerical value of mass rate of flow at the entrance to the mixing chamber
ANA	···rat m·····	
ANB	$\cdot \cdot \frac{r_{b}-r_{at}}{r_{bt}-r_{at}} \pi \cdot \cdot \cdot \cdot$	function angles for numerical integration of total enthalpy
ANC	0	
BETA	Momentum Rate	numerical value of the momentum rate at the entrance to the mixing chamber
	$\frac{r_b-r_a}{\pi}$	
CHIA	r _{at} -r _a	constants of integration for energy equation
GHIB	<u>π</u>	
CONST	$\frac{(\mathbf{T}_{\mathbf{p}} - \overline{\mathbf{T}})\overline{\mathbf{V}}}{(\mathbf{V}_{\mathbf{p}} - \overline{\mathbf{V}})\overline{\mathbf{T}}}.$	proportionality constant between axial fluid temperature and axial fluid velocity after all spreading radii have reached their respective limits
DA	$\frac{(\mathbf{r}_{b}-\mathbf{r}_{a})\pi}{100\mathbf{r}_{s}}$	incremental changes in the angles during numerical integration of total enthalpy rate
DB	$\frac{(\mathbf{r}_{b}-\mathbf{r}_{a})}{100(\mathbf{r}_{b}-\mathbf{r}_{a})}$	cotal eucualbh Lace

DELTA..... numerical value of Bernoulli's

constant for secondary fluid

$DIST(I) \underbrace{X}_{\mathbf{r}_{a_{\mathbf{p}}}}$	non-dimensional ratio of axial distance from the entrance to the mixing chamber to that of the peripheral diameter of the central jet
DP(I)	the change in the non-dimensional value of P(I) between a given cross-section and the entrance to the mixing chamber
$\frac{T_p - T_s}{2}$	one-half of the difference between the central and peripheral temp- erature
$v_p - v_s$	one-half of the difference between the central and peripheral velo- city
DVPv _p - \overline{\overline{v}}	numerical difference between the axial fluid velocity and the final uniform velocity
$DX(I)$ $\Delta\left(\frac{X}{r_a}\right)$	the change in the non-dimensional ratio DIST(I) between a given cross-section and the previously computed cross-section
ETA + ZETA(H) _x	numerical value of total enthalpy rate at a given cross-section
FLAG	constant used to ensure that the first correct value of CONST is used throughout the program
GAMMA	numerical value of Bernoulli's constant for the central fluid
$\pi \rho c_p V_s r_a^2$	numerical value of the total en- thalpy rate at the entrance to the mixing chamber
PI Momentum rate ra	numerical value of the momentum rate for uniform flow at exit
P(I)p	non-dimensional ratio of pressure to one-half times the density times the initial secondary fluid velo- city squared

	Momentum rate x Km	numerical multiple of the final momentum rate at any given cross-section
RA(I)	r _a R _a .	non-dimensional ratio of the central radius describing velocity core boundary at a given cross-section to that of the central jet radius
RAT(I)	$\frac{r_{at}}{r_{a_o}} = R_{at}$	non-dimensional ratio of the central radius describing temperature core boundary at a given cross-section to that of the initial central jet radius
RB(I)	$\frac{\mathbf{r}_{\mathbf{b}}}{\mathbf{r}_{\mathbf{a}_{\mathbf{o}}}} = \mathbf{R}_{\mathbf{b}} \cdot \cdots \cdot \mathbf{r}$	non-dimensional ratio of the peripheral radius describing velocity jet boundary at a given cross-section to that of the initial central jet radius
RBT(I)	$\frac{r_{bt}}{r_{a_o}} = R_{bt} \cdots$	non-dimensional ratio of the peripheral radius describing temperature jet boundary at a given cross-section to that of the initial jet radius
RS	$\frac{\mathbf{r}_{s}}{\mathbf{r}_{a_{o}}} = \mathbf{R}_{s}$	ratio of peripheral radius of mixing chamber to the initial jet radius
	ra ra	limits of integration for the continuity equation and the momentum equation
RZ	.r _z	reference radius during numeri- cal integration of the total enthalpy rate
SIG(J)	.h Δm	incremental numerical segments whose total is ZETA [ZETA = Σ Sig(J)]
TAVE	$\frac{T_p + T_s}{2} = T_{ave} \cdots$	average value of central and peripheral temperature
TBAR	.Ť	final uniform temperature at exit

TAU + OMEGA. $\frac{\text{Momentum}}{\pi \rho \text{V}_{\text{s}_{\text{o}}}^{2} \text{r}_{\text{a}_{\text{o}}}^{2}} = M$	numerical value of the momentum rate at a given cross-section
TAU + SIGMA. $\frac{m_x}{\pi \rho V_s r_a^2}$	numerical value of the mass flow rate at a given cross-section
TP(I)Tp	numerical value of the central fluid temperature above the initial secondary fluid temperature at the entrance to the mixing chamber
TS(I)T _s	numerical value of peripheral fluid temperature above the initial secondary fluid temperature at the entrance to the mixing chamber
$VAVEV_p + V_s$ = $Vave$	average value of the central and peripheral velocity
VBAR	final uniform velocity at exit
$VP(I) \cdots v_{\underline{v}_{\underline{s}_{\bullet}}} = V_{\underline{p}} * \cdots$	numerical ratio of central fluid velocity to initial secondary fluid velocity at the entrance to the mixing chamber
$VS(I) \dots V_{S_{s_o}} = V_{S}^* \dots$	numerical ratio of peripheral fluid velocity to initial secondary fluid velocity at the entrance to the mixing chamber

1. Introduction

The majority of analyses of the physical properties of fluids in ejectors have used a one-dimensional approach in which uniform properties are assumed at the entrance to the mixing chamber which is of sufficient length for the properties to again become uniform at the exit. For example. consider a primary fluid flowing along the central axis of a cylindrical ejector and a secondary fluid flowing parallel to and completely surrounding it. as shown in Fig. 1. fluids are separated by a circular boundary. At the entrance to the mixing chamber the boundary between the two fluids is removed and, at this initial cross-section, both the primary and the secondary fluids have uniform but different velocities. As the primary and secondary fluids flow axially through the mixing chamber, the fluids mix and the physical properties of each one of them are affected by the physical properties of the adjacent fluid.2

It is the purpose of this investigation, by use of a high speed digital computer and Fortran Programming Language, to predict what the properties in the partially mixed, non-

¹S. Pai, Fluid Dynamics of Jets, D. Van Nostrand Co., Inc., New York, 1954

²R. A. Smith, "Theory and Design of Simple Ejectors", Some Aspects of Fluid Flow, Edward Arnold and Co., London, 1951

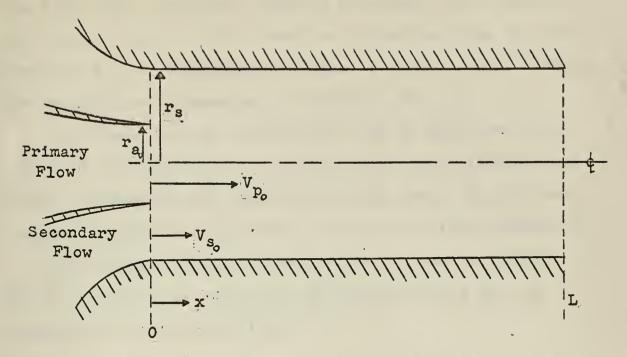


Fig.1 Ejector Geometry and Initial Flow Parameters.

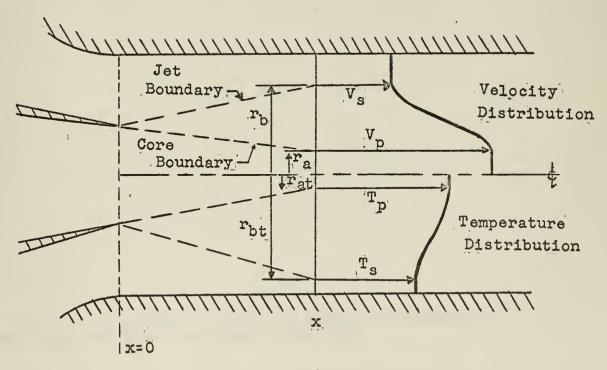


Fig. 2 Typical Velocity and Temperature Profiles

uniform sections of the stream will be. 3 Consideration of the fluid flow mechanisms, such as the shear stress within the fluids, leads to the concept of a profile shape for the properties at a given cross-section. A typical profile shape for velocity and temperature is shown in Fig. 2.

The first problem considered is one in which the velocities of the primary and secondary fluids are different but their temperatures and densities are the same. The Fortran Program developed to solve this problem is called EJECTMIX I.

The second problem, considered in the program EJECT-MIX II, studies the variations in the velocities and the temperatures of the two fluids.

³D. D. McCracken, A Guide to FORTRAN Programming, John Wiley and Sons Inc., New York, 1961

2. Ejector Analysis

In order to analyse the behavior of the physical properties in the mixing chamber of an ejector there are several possible analytic approaches.

The first possible approach is a one-dimensional overall analysis in which uniform properties are assumed at the entrance and uniform properties of the completely mixed fluids are assumed at the exit of the mixing chamber. With this analysis, the region in which mixing of the primary and secondary fluids takes place is not considered. The only regions where the physical properties are studied are at the entrance to the mixing chamber and after the point where uniform flow exists.

A second possible approach is that of an internal analysis which is based on the actual fluid mechanisms. This approach requires the examination of an element of fluid and the forces which are acting upon it. The difficulty here lies in the inability to acquire a usable analytic expression for the shear stress acting upon the element of fluid.

A third approach, the one used in this thesis, is the generation of compatible solutions for the physical properties of the fluids at representative axial cross-sections by means of consideration of Conservation of Mass, Momentum, Bernoulli's Equation and the Energy Equation. In order to apply the above equations to the fluid in the mixing chamber, certain basic assumptions as to the nature of the flow in the

mixing chamber must be made.

First of all, the flow in the mixing chamber is assumed to be divided into regions which are shown in Fig. 3a and Fig. 3c. These regions are defined by the central core boundary and the expanding jet boundary. There are similar velocity and temperature profiles which consist of uniform portions at the central axis and the periphery of the mixing chamber, which are connected by a cosine shaped profile. The assumed profile shapes are shown in Fig. 3b and Fig. 3d. Assuming profile shapes, negligible boundary effects, constant pressure across any given cross-section, and constant temperature until a mixing region is reached, the previously mentioned equations can then be used.

The first equation considered is the Equation of Continuity

$$\dot{m} = \int_{0}^{r_S} \rho V dA = Constant$$

For a typical profile shape, as shown in Fig. 3e, the Equation of Continuity becomes

$$\dot{m} = 2\pi\rho \left(\int_{0}^{\mathbf{r}_{a}} \mathbf{V} \mathbf{p} \, \mathbf{r} \, d\mathbf{r} + \int_{\mathbf{r}_{a}}^{\mathbf{r}_{b}} \left[\mathbf{V}_{a\mathbf{v}e} + d\mathbf{V} \, \cos \left(\frac{\mathbf{r} - \mathbf{r}_{a}}{\mathbf{r}_{b} - \mathbf{r}_{a}} \pi \right) \right] \, \mathbf{r} \, d\mathbf{r} + \int_{\mathbf{r}_{b}}^{\mathbf{r}_{s}} \mathbf{V}_{s} \, \mathbf{r} \, d\mathbf{r} \right)$$

Integrating and evaluating the integral gives

$$\dot{m} = \pi \rho \left(v_{p} r_{a}^{2} + v_{ave} \left[r_{b}^{2} - r_{a}^{2} \right] - 4 dv \left[\frac{r_{b} - r_{a}}{\pi} \right]^{2} + v_{s} \left[r_{s}^{2} - r_{b}^{2} \right] \right)$$

Dividing through the entire equation by $\pi \rho V_s r_a^2$, the

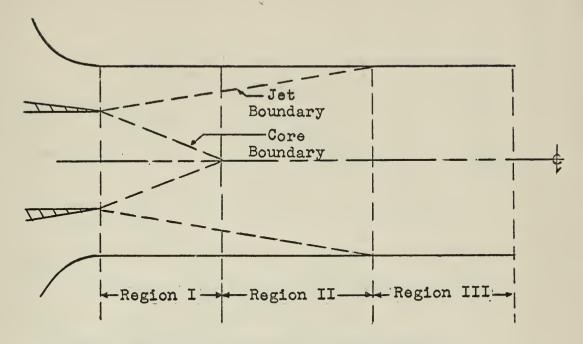


Fig. 3a Possible Spread Rate Configuration

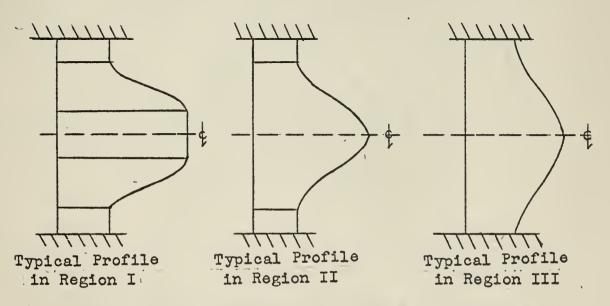


Fig. 3b Typical Profiles for Regions of Fig. 3a

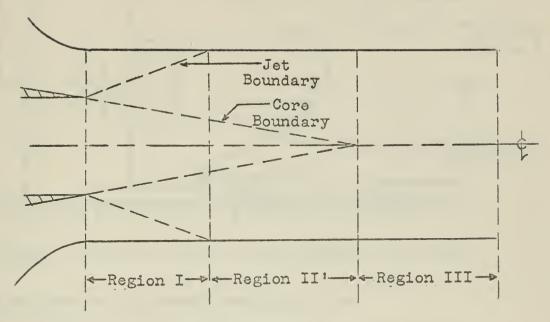


Fig. 3c Possible Spread Rate Configuration

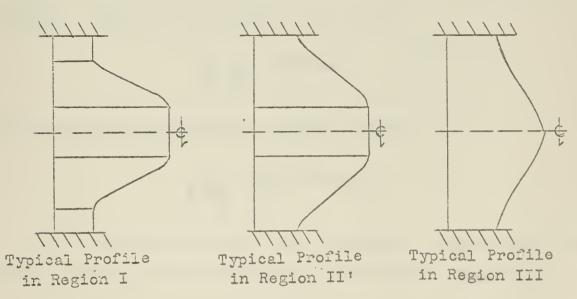


Fig. 3d Typical Profiles for Regions of Fig. 3c

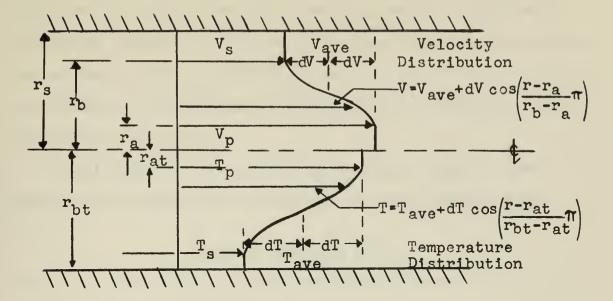


Fig. 3e Typical Profiles with Equation Parameters

equation takes on the non-dimensional form

$$\frac{\mathbf{r}_{a}}{\pi \rho v_{s_{a}}^{r_{a}^{2}}} = \frac{v_{p_{x}}}{v_{s_{a}}^{2}} \frac{\mathbf{r}_{a_{x}}^{2} + v_{ave_{x}}}{\mathbf{r}_{a_{a}}^{2}} \frac{(\mathbf{r}_{b_{x}}^{2} - \mathbf{r}_{a_{x}}^{2})}{\mathbf{r}_{a_{a}}^{2}} - 4 \frac{dv_{x}}{v_{s_{a}}} \left(\frac{\mathbf{r}_{b_{x}}^{2} - \mathbf{r}_{a_{x}}^{2}}{\pi \mathbf{r}_{a_{a}}^{2}}\right) + \frac{v_{s_{x}}}{v_{s_{a}}} \frac{(\mathbf{r}_{s}^{2} - \mathbf{r}_{b_{x}}^{2})}{\mathbf{r}_{a_{a}}^{2}}$$

The next consideration is that of Bernoulli's Equation along a streamline in the uniform velocity portions of the profile. Bernoulli's Equation states that

$$\frac{p}{\rho} + \frac{v^2}{2} = Constant$$

In non-dimensional form the equation becomes

$$\frac{p}{\frac{1}{2}\rho V_s^2} + \frac{V^2}{V_s^2} = Constant$$

The constant associated with Bernoulli's Equation in the primary core is found by evaluating Bernoulli's Equation in

the non-dimensional form along the axis at the entrance to the mixing chamber. Similarly, the constant associated with the secondary cone is determined at the entrance to the mixing chamber. These values will be used in conjunction with the Momentum Equation.

Considering the same profile which was used in the Equation of Continuity and solving for the Momentum rate

Momentum rate =
$$\int \rho V^2 dA$$

over the entire cross-section the Momentum Rate Equation be-

Momentum Rate =
$$2\pi\rho \left(\int_{0}^{\mathbf{r}a} V_{\mathbf{p}}^{2} \mathbf{r} d\mathbf{r} + \int_{\mathbf{r}_{\mathbf{b}}}^{\mathbf{r}_{\mathbf{b}}} \left[V_{\mathbf{a}}v_{\mathbf{c}} + dV_{\mathbf{c}}\cos\left(\frac{\mathbf{r}-\mathbf{r}_{\mathbf{a}}}{\mathbf{r}_{\mathbf{b}}-\mathbf{r}_{\mathbf{a}}}\right)\right]^{2} \mathbf{r} d\mathbf{r} + \int_{\mathbf{r}_{\mathbf{b}}}^{\mathbf{r}_{\mathbf{s}}} V_{\mathbf{s}}^{2} \mathbf{r} d\mathbf{r}\right)$$

Integrating and evaluating the integral

Momentum Rate =
$$\pi \rho \left(v_p^2 r_a^2 + v_{ave} \left[r_b^2 - r_a^2 \right] - 8 v_{ave} dv \left[\frac{r_b - r_a}{\pi} \right]^2 + dv^2 \left[\pi r_b \left(\frac{r_b - r_a}{\pi} \right) - \frac{\pi^2}{2} \left(\frac{r_b - r_a}{\pi} \right)^2 \right] v_s^2 \left[r_s^2 - r_b^2 \right] \right)$$

Dividing through the entire equation by $\pi_p V_{s_0}^2 r_{a_0}^2$ puts the equation in the non-dimensional form

$$\frac{\text{Momentum Rate}}{\pi \rho \, V_{s}^{2} r_{a}^{2}} = \frac{V_{p}^{2}}{V_{s}^{2}} \frac{r_{a}^{2}}{r_{a}^{2}} + \frac{V_{ave}^{2}}{V_{s}^{2}} \frac{(r_{b}^{2} - r_{a}^{2})}{r_{a}^{2}} - 8 \frac{V_{ave}}{V_{s}^{2}} \frac{dV_{x}}{v_{x}^{2}} \left(\frac{r_{b}^{2} - r_{a}}{\pi \, r_{a}}\right)^{2}$$

$$\frac{dV_{x}^{2}}{V_{s_{o}}^{2}} \left(\pi \frac{r_{b_{x}}}{r_{a_{o}}^{2}} (r_{b_{x}} - r_{a_{x}}) - \frac{\pi^{2}}{2} \left[\frac{r_{b_{x}} - r_{a_{x}}}{\pi r_{a_{o}}} \right]^{2} \right) + \frac{V_{s_{x}}^{2}}{V_{s_{o}}^{2}} \frac{r_{s}^{2} - r_{b_{x}}^{2}}{r_{a_{p}}^{2}}$$

The Momentum Equation is then applied to the ejector in the axial direction. Neglecting shear stress at the ejector walls,

$$\Delta p \pi r_s^2 = \Delta (Momentum Rate)$$

Defining a non-dimensional Momentum Rate by dividing by $\text{To}_{s_{0}}^{2} \text{r}_{a_{0}}^{2}$, we obtain,

$$\frac{\Delta p}{\rho V_{s_o}^2} \frac{r_s^2}{r_{a_o}^2} = \Delta \dot{M}$$

Defining a non-dimensional pressure difference, Δ p*, as

$$\Delta p^* = \frac{\Delta p}{\frac{1}{2}\rho V_s^2} = \Delta \dot{H} \frac{2r_a^2}{r_s^2}$$

where $\Delta p = p_X - p_{X=0}$ and $\Delta \dot{M} = \dot{M}_X - \dot{M}_{X=0}$.

The final equation used is the Energy Equation in which the heat transferred to the surroundings is assumed to be zero. The difference in geo-potential energy is negligible and, lastly, the change in kinetic energy is negligible in comparison with the Enthalpy Rate. Thus the Energy Equation becomes

$$\dot{H} = \int d\dot{H} = \int hd\dot{m} = 2\pi \rho c_p \int TV rdr = Constant$$

Using the same profile shapes as before, the Enthalpy
Rate for a typical axial cross-section becomes

$$\begin{split} & \dot{\mathbf{H}} = 2\,\pi\rho\,\mathbf{c}_{\mathrm{p}} \left(\int_{0}^{\mathbf{r}_{\mathrm{a}}} \mathbf{T}_{\mathrm{p}} \,\,\mathbf{V}_{\mathrm{p}}\mathbf{r} \,\,\mathrm{d}\mathbf{r} + \int_{\mathbf{r}_{\mathrm{a}}}^{\mathbf{r}_{\mathrm{a}}} \mathbf{T}_{\mathrm{p}} \,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{a}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{ave}} + \mathrm{d}\mathbf{T} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\left[\mathbf{V}_{\mathrm{ave}} + \mathrm{d}\mathbf{V} \,\,\cos\!\left(\frac{\mathbf{r} - \mathbf{r}_{\mathrm{a}}}{\mathbf{r}_{\mathrm{b}} - \mathbf{r}_{\mathrm{a}}}\right) \right] \,\,\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathbf{v} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathbf{v} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathbf{v} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathbf{v} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{s}} \,\,\mathrm{d}\mathbf{r} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{b}} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{\mathbf{r}_{\mathrm{b}}} \mathbf{T}_{\mathrm{b}} \,\,\mathrm{d}\mathbf{r} \,\,+ \\ & \int_{\mathbf{r}_{\mathrm{b}}}^{$$

The second term of the Enthalpy Rate Equation, namely,

$$2\pi\rho c_{p} \int_{r_{at}}^{r_{bt}} \left[V_{ave} + dV \cos \left(\frac{r - r_{a}}{r_{b} - r_{a}} \pi \right) \right] \left[T_{ave} + dT \cos \left(\frac{r - r_{at}}{r_{bt} - r_{at}} \pi \right) \right] r dr$$

was solved by numerical integration. The interval between $r_{\rm at}$ and $r_{\rm bt}$ was divided into 100 increments and summed.

The other integrals which make up the total value of the Enthalpy Rate are integrated and evaluated giving

In order to place this in non-dimensional form, the equation was divided by $\pi_p c_p V_{s_o} r_{a_o}^2$. Thus the integral for numerical integration becomes

$$\int_{R_{at}}^{R_{bt}} \left[\frac{\overline{v}_{ave_{x}}}{\overline{v}_{s_{o}}} + \frac{dv_{x}}{\overline{v}_{s_{o}}} \cos \left(\frac{r - r_{ax}}{r_{b_{x}} - r_{ax}} \pi \right) \right] \left[\frac{T_{ave_{x}}}{T_{ave_{x}}} + dT_{x} \cos \left(\frac{r - r_{at_{x}}}{r_{bt_{x}} - r_{at_{x}}} \pi \right) \right] \frac{r}{r_{a_{o}}} d \left[\frac{r}{r_{a_{o}}} \right]$$

Non-dimensionalizing the evaluated portion of the Enthalpy Rate gives

$$\frac{V_{p_{x}}}{V_{s_{o}}}T_{p_{x}}\frac{r_{a}t_{x}^{2}}{r_{a_{o}}^{2}} + \frac{V_{p_{x}}}{V_{s_{o}}}T_{ave_{x}}\frac{(r_{a_{x}}^{2}-r_{a}t_{x}^{2})}{r_{a_{o}}^{2}} +$$

$$\frac{2V_{p_{x}}}{V_{s_{o}}}dT_{x}\left(\frac{r_{b}t_{x}^{-r}r_{a}t_{x}}{\pi}\right)\frac{r_{a_{x}}}{r_{a_{o}}^{2}}\sin\left(\frac{r_{a_{x}}^{-r}r_{a}t_{x}}{r_{b}t_{x}^{-r}r_{a}t_{x}}\right) +$$

$$\frac{2V_{p_{x}}}{V_{s_{o}}}dT_{x}\left(\frac{r_{b}t_{x}^{-r}r_{a}t_{x}}{\pi}\right)\left(\cos\left[\frac{r_{a_{x}}^{-r}r_{a}t_{x}}{r_{b}t_{x}^{-r}r_{a}t_{x}}\right]^{-1}\right) +$$

$$\frac{V_{s_{x}}}{V_{s_{o}}}T_{ave_{x}}\frac{(r_{b}t_{x}^{2}-r_{b_{x}}^{2})}{r_{a_{o}}^{2}}\frac{-2V_{s_{x}}}{V_{s_{o}}}dT_{x}\left(\frac{r_{b}t_{x}^{-r}r_{a}t_{x}}{\pi}\right)\frac{r_{b_{x}}}{r_{a}}\sin\left(\frac{r_{b_{x}}^{-r}r_{a}t_{x}}{r_{b}t_{x}^{-r}r_{a}t_{x}}\right)$$

$$\frac{V_{s_{x}}}{V_{s_{o}}}T_{a_{o}}\frac{(r_{b}t_{x}^{2}-r_{b}t_{x}^{2})}{V_{s_{o}}}\left(1 -\cos\left[\frac{r_{b_{x}}^{-r}r_{a}t_{x}}{r_{b}t_{x}^{-r}r_{a}t_{x}}\right]\right) + \frac{V_{s_{x}}}{V_{s_{b}}}T_{s_{x}}\frac{(r_{s}^{2}-r_{b}t_{x}^{2})}{r_{a_{o}}^{2}}$$

3. Method

The equations employed in EJECTMIX I and EJECTMIX II were used in the following manner. At a given axial position, a core boundary (r_a) is assumed. Primary and secondary velocities $(V_p \text{ and } V_s)$ are assumed which will be compatible with the Bernoulli Equation for the entrance to the mixing chamber. A jet boundary (r_b) is assumed and the conditions are checked for Conservation of Mass by means of the Continuity Equation. The primary and secondary velocities are corrected by an iterative process until a compatible solution is found.

The velocities found by the Continuity Equation are then used to solve for the pressure at the cross-section under consideration. Pressure changes determined from Bernoulli's Equation along streamlines in the uniform flow velocity regions are compared with the pressure change found from the overall Momentum Rate. If the pressure is found to be incompatible, the jet boundary (rh) is corrected and once again the Equation of Continuity is used in order to determine compatible central and peripheral velocities. The values found by the Continuity Equation are then used to find a new value of the Momentum Rate, which, in turn, determines a new pressure change which can be used in Bernoulli's Equation to check the velocities found by Continuity. This process repeats itself until the core and jet boundaries (r and r), the central and peripheral velocities (V_p and V_s) and the pressure change are all compatible in the three basic equa-

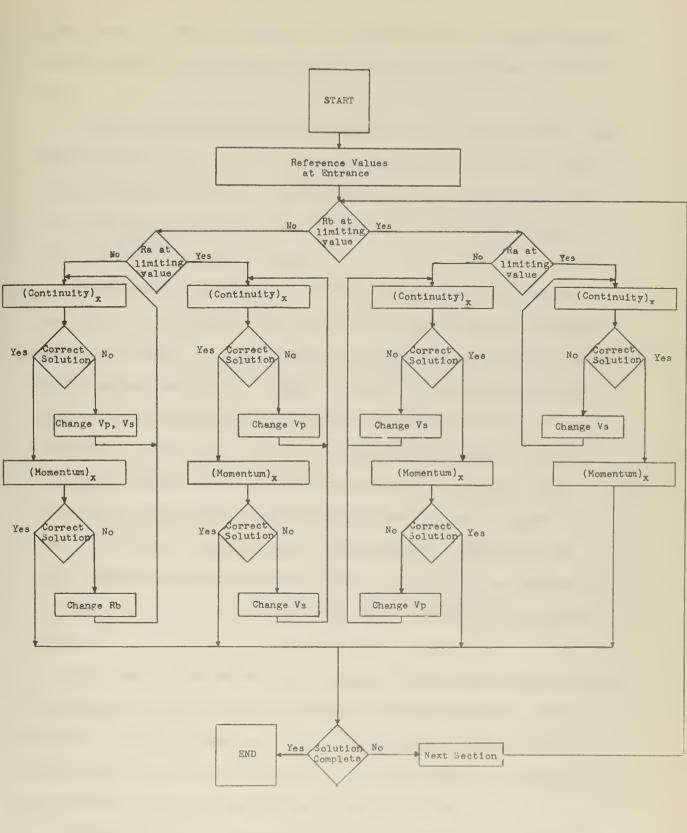


Fig. 4 Block Diagram for EJECTMIX I

tions used. Then the process is repeated for the next crosssection which is displaced axially in the direction of fluid flow.

After several cross-sections have been investigated, the core boundary (r_a) or the jet boundary (r_b) may reach their limiting value, that is, the central core boundary (r_a) may go to zero or the peripheral jet boundary (r_b) may reach the mixing chamber boundary (r_a) .

Considering the case of either one of the boundaries reaching its limiting value while the other boundary remains within its limit, the scheme for finding the compatible solution remains exactly the same as that used when both boundaries were within limits, with the exception of the role of Bernoulli's Equation. Since the flow field will no longer be uniform where the boundary has reached its limit, the streamline along which Bernoulli's Equation was assumed to have a constant value will no longer exist. With this in mind, Bernoulli's Equation will only be taken into account in the uniform flow portion which has not reached its limiting value.

When both boundaries have reached their respective limiting values, no additional restrictions are required other than the overall Momentum Rate. Compatible solutions are then found using fixed increments of the central velocity as the criteria for the particular cross-section.

EJECTMIX II is basically the same program as EJECTMIX I

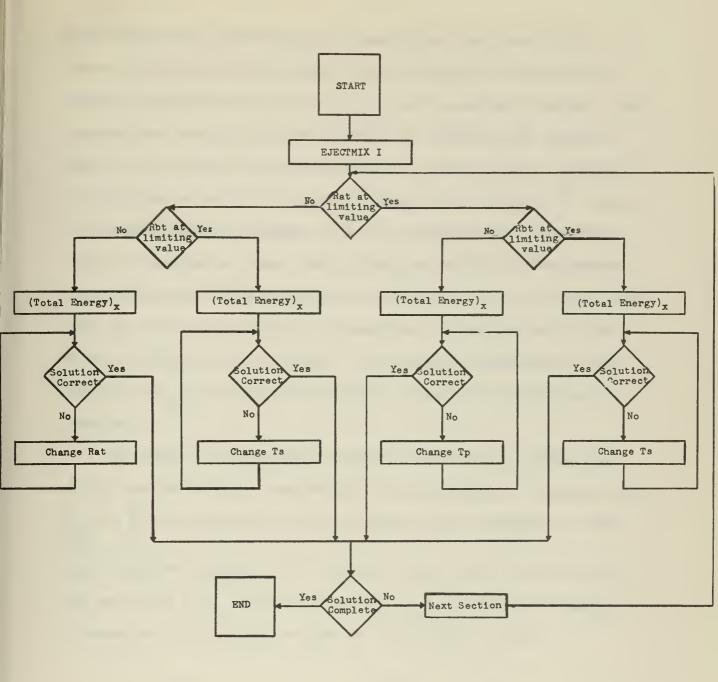


Fig. 5 Block Diagram for EJECTMIX II

with additional restrictions placed upon the flow field. These additional restrictions take the form of variations in the temperatures of the primary and secondary fluids. The temperature boundaries are assumed to spread more rapidly than the velocity region boundaries. This has been verified by experiments on jets of gases flowing in ejectors. Also, the temperature is assumed to be a constant until the temperature boundaries reach their limiting values. The temperature boundaries are assumed and the value of the energy equation at the cross-section in question is compared with that of the initial cross-section. The central temperature core boundary (rat) is corrected until a compatible solution is obtained.

In order to determine the axial position on which each of the representative compatible solutions lie, a spread rate $\left[\frac{d}{d_x}(r_b)\right]$ is assumed for the peripheral jet boundary. When this boundary reaches its limiting value, it is assumed that the pressure will continue varying as a smooth curve until it reaches its limiting value in the mixing chamber.

¹⁴D. Küchemann and J. Weber, Aerodynamics of Propulsion, McGraw-Hill Book Co., Inc., New York, 1953

4. Results

The data which was obtained using EJECTMIX I and EJECTMIX II is presented in graphical form in Appendix 2 and in tabular form in Appendix 3. The properties obtained are presented in groups according to the ratio of the radius of the peripheral boundary to the central jet radius. The values of this given ratio are 1.5. 3.0 and 10.0.

These graphs may be entered with the known physical dimensions of the ejector mixing chamber and the velocity ratio. The ratio of the initial peripheral radius to the central jet radius of ten to one gives an actual area ratio of 100 to one and thus approaches the condition whereby the peripheral fluid actually would be unbounded.

The graphical solutions shown are those in which the fluid was assumed to return to a uniform flow after it had passed down an axial distance equal to ten times the peripheral diameter. The data and graphs are presented as functions of axial distance divided by initial central jet radius (X/r). Tabulated data shown in Appendix 3 is the computer output which was used to produce these graphs.

In the course of finding compatible solutions, a temperature difference of 100 degrees was used. By varying only the temperature, the solutions obtained for temperature were directly proportional to each other. With this in mind, the temperature difference for any case can be determined by using a proportionality constant and a 100 degree temperature

difference. Temperatures are measured above a reference temperature which is the secondary fluid temperature at the initial cross-section.

The pressure term as used in Bernoulli's Equation is not significant in its absolute value since it cancels out of the equation when used in these programs. Its significance lies in the change of the non-dimensional pressure term. With each specific case an initial non-dimensional pressure can be determined. This non-dimensional pressure will be a function of the absolute velocities, the pressure and the fluid flowing in the ejector.

Since the initial peripheral velocity ratio is equal to one, a change in the non-dimensional pressure of one, before the velocity jet boundary reaches its limiting value, leads to a zero velocity ratio through the Bernoulli Equation. Any increase in the non-dimensional pressure beyond the value of one leads to compatible solutions in which the peripheral velocity becomes negative. This phenomenon is dependent upon the velocity ratio and the cross-sectional area of the central and peripheral jets.

Negative peripheral velocity ratios first appeared in the range of the values studied at an initial central velocity ratio of ten and an area ratio less than 100 to one. The flow pattern which exists when negative peripheral velocity ratios are generated in the compatible solution is shown in Fig. 6.

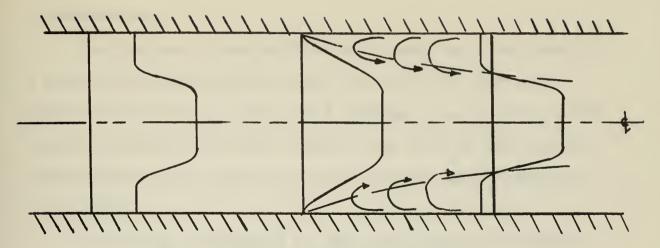


Fig. 6 Profiles and Flow Pattern with Negative Peripheral Velocities

Throughout most of the program accuracy of one-half of one percent is required in order for the solution to be considered acceptable. This criterion fails during the transition of the peripheral velocity ratio term through its zero values. For this portion of the program accuracy of plus or minus one one-hundredth for the non-dimensional velocity term is required. This change in the criterion ensures that a finite and acceptable error can be established for any value of the peripheral velocity ratio.

The final piece of data presented by the program is the Momentum Factor. This term gives that multiple of the final momentum that exists at any point.

5. Conclusions

The programs presented here represent the first step in a series of programs which would eventually describe the physical properties of any fluid flowing in an ejector. This logical continuation would require that work be done on the compressible fluid problem at both subsonic and supersonic velocities.

The programs contained in this work solve the ejector problem for two incompressible fluids of the same density whose physical properties are initially different. The data obtained is presented here in graphical and tabular form.

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APPENDIX I

Appendix I contains a listing, in FORTRAN language, of the programs EJECTMIX I and EJECTMIX II.

PROGRAM EJECTMIX 1

DIMENSION RA(500), RB(500), VP(500), VS(500), P(500), PSI(500), CP(500)

READ 101 (VP(1), RS)

101 FORMAT (2F15.0)

VS(1) = 1.0

P(11) = 10.0

DP(1) = 0.0

RA(11) = 1.0

RB(1) = 1.0RB(2) = 1.03

•

ALPHA = VP(1)*RB(1)**2 + (RS**2 - RB(1)**2)

BETA = VP(1)**2*RB(1)**2 + (RS**2 - RB(1)**2)

GAMMA = P(1) + VP(1) **2

DELTA = P(11) + 1.0

THETA = GAMMA - DELTA

PI = ALPHA ** 2/RS ** 2

PSI(1) = BETA/PI

WRITE OUTPUT TAPE 4,102 WRITE OUTPUT TAPE 4,103

PRINT 133, RA(I), RB(I), OP(I), VP(I), VS(I), PSI(I)

102 FORMAT (11X, 7HCENTRAL, 8X, 10HPERIPHERAL, 7X, 8HPRESSURE, 8X, 17HCENTRAL, 8X, 1CHPERIPHERAL, 7X, 8HMCMENTUM)

103 FORMAT (12x, 6HRADIUS, 10x, 6HRADIUS, 10x, 6HCHANGE, 9x,

18HVELOCITY, 8X, 8EVELOCITY, 9X, 6HFACTOR//)

104 RA(1 + 1) = RA(1) - 0.01

VP(I + 1) = VP(I)VS(I + 1) = VS(I)

+ - -

IF (RS - RB(II) 122, 122, 105

105 IF (RA(II)) 137, 106, 106

106 CHI = (RB(I) - RA(I))/3.1415926

107 TAU = VP(I)*RA(I)**2 + VS(I)*(RS**2 - RB(I)**2)

RX = RA(I)

RY = RB(I)

```
108 \text{ DV} = (\text{VP}(1) - \text{VS}(1))/2.0
```

$$VAVE = VS(I) + DV$$

$$109 \text{ VP(I)} = \text{VP(I)} - 0.000007$$

$$VS(I) = SQRTF(VP(I)**2 - THETA)$$

111
$$VP(I) = VP(I) + 0.00001$$

$$VS(I) = SQRTF(VP(I)**2 - THETA)$$

$$P(I) = P(I) + DP(I)$$

```
114 IF (0.995*(DELTA - P(I)) - VS(I)**2) 135,136,116
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               OMEGA = VAVE*(RY**2 - RX**2) - 4.0*0V*CHI**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  IF (ALPHA - FNECA - TAU + 0.001)125,126,126
                                     RR(1 + 1) = 2.0*RR(1) - RR(1 - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CHI = (RS - RA(I))/3.1415926
                                                                                                                                                                                                                                                                                                                                                                                                                        124 DV = (VP(I) - VS(I))/2.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   125 \text{ VS}(1) = \text{VS}(1) - \text{C.CC007}
                                                                                                                                                                                          116 RB(1) = RB(1) - 0.0001
                                                                                                                 RE(1) = RB(1) + C.COC1
                                                                                                                                                                                                                                                                    122 IF(RA(I)) 147, 123, 123
                                                                                                                                                                                                                                                                                                                                                                                                                                                               TAU = VP(I)*RA(I)**2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VAVE = VS(1) + CV
                                                                                                                                                                                                                                                                                                       123 RB(11) = RS
                                                                                                                                                                                                                                                                                                                                               RX = RA(I)
                                                                                                                                                      GO TO 117
                                                                          GO TO 132
                                                                                                                                                                                                                               117 GO TO 106
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               GC TC 124
                                                                                                                                                                                                                                                                                                                                                                                      RY = RS
```

126 IF (ALPHA - CMECA - TAU - C.001) 128,128,127

127 VS(1) = VS(1) + 0.0001

GO TO 124

128 TAU = VP(1)**2*RA(1)**2

129 SIGMA = VAVE ** 2 = (RY ** 2 - RX ** 2) - 8.0 * VAVE * DV * C + I ** 2

10V**2*CHI*RY*3.1415926 - 4.9348022*CHI**2*DV**2

OP(1) = (BETA - SIGMA - TAU) / (0.5*RS**2)

P(1) = P(1) + OP(1)

IF (1.005*(SANMA - P(I)) - VP(I) **2) 131,132,130

130 IF (0.995*(GAMMA - P(I)) - VP(I) **2) 132,132,135

131 VP(1) = VP(1) - 0.0001

GC TC 124

132 PSI(I) = (SIGMA + TAU)/PI

 $RB(I + 1) = 2.0 \times RB(I) - RB(I - 1)$

PRINT 133, RA(I), RB(I), DP(I), VP(I), VS(I), PSI(I)

133 FORMAT (5x, 6£16.7)

GO TO 104

135 VP(I) = VP(I) + 0.0001

GO TO 124

137 TAU = VS(I)*(RS**2 - RB(I)**2)

RA(I) = 0.0

x = C.0

RY = RB(1)

CHI = RB(1)/3.1415526

138 DV = (VP(1) - VS(1))/2.0

VAVE = VS(I) + EV

OMEGA = VAVE*(RY**2 - RX**2) - 4.0*DV*CHI**2

IF (ALPHA - CMEGA - TAU + C.001) 140,142,139

139 IF (ALPHA - CMEGA - TAU - 0.001) 142,142,141

140 VP(1) = VP(9) - 0.00007

GC TC 138

141 VP(I) = VP(I) + 0.0001

GO TO 133

142 IAU = VS(1)**2*(RS**2 - RP(1)**2)

SIGNA = VAVE**2*(RY**2 - RX**2) - 8.0*VAVE*DV*CHI**2

1DV**2*CHI*RY*3.1415926 - 4.9348022*CHI**2*CV**2

DP(1) = (RETA - SIGNA - TAU)/(0.5*RS**2)

P(1) = P(1) + GP(1)

IF (1.005*(DELTA - P(I)) - VS(I)**2) 145,144,143

143 IF (0.995*(DELTA - P(I)) - VS(I) **2) 144,144,146

144 RB(I + 1) = RB(I) + 0.01

60 10 132

145 VS(1) = VS(1) - 0.0001

GO TO 137

146 VS(I) = VS(I) + 0.0001

60 10 137

147 RA(I) = 0.0

RX = 0.0

RB(I) = RS

RY = RS

TAU = 0.0

CHI = RS/3.1415926

 $VAVE = VS(I) + \Gamma V$

148 DV = (VP(I) - VS(I))/2.0

OMEGA = VAVE*(RY**2 - RX**2) - 4.0*CV*CHI**2

IF (ALPHA - CMEGA + 0.001)150,149,149

149 IF (ALPHA - CMEGA - 0.001) 152,152,151

150 VS(I) = VS(I) - 0.00007

GO TO 148

151 VS(I) = VS(I) + 0.0001

60 10 148

152 SIGMA = VAVE**2*(RY**2 - RX**2) - 8.0*VAVE*DV*CFI**2 +

1DV**2*CHI*RY*3.1415926 - 4.9348022*CHI**2*DV**2

DF:11) = (BETA - SIGNA - TAU)/(0.5*RS**2)

P(11) = P(11) + DP(11)

PSI(I) = (SIGNA + TAU)/PI

PRINT 153, RA(I), RE(I), OP(I), VP(I), VS(I), PSI(I)

153 FORMAT (5X,6216.7)

VP(1 + 1) = VP(1) - 0.01

IF (VP(I) - VS(I)) 134,154,154

VS(1 + 1) = VS(1) + 0.0001

154 I = I + 1

GO TO 147

134 STOP

END

END

PROGRAM EJECTMIX II

DIMENSION RA(500), RB(500), VP(500), VS(500), P(500), PSI(500),

10P(500), TP(5C0), TS(500), DIST(500), DX(500), RAT(500),

2RBT(500), SIG(500)

READ 101 (VP(1), RS, TP(1))

101 FORMAT (3F10.0)

PARAB1 = 0.002

70 P(11) = 10.0DP(11) = 0.0

TS(11) = 0.0

VS(1) = 1.0RA(11) = 1.0

RB(1) = 1.0

RAT(1) = 1.0 RB(2) = 1.1

RBT(11) = 1.0

RBT(0) = 1.0

DIST(1) = 0.0

FLAG = 0.0

PARAB2 = 1.3 *PARAB1

II

ALPHA = VP(1)*RB(1)**2 + (RS**2 - RB(1)**2)

BETA = VP(1) **2*RB(1) **2 + (RS**2 - RB(1) **2)

GAMMA = P(1) + VP(1) **2

DELTA = P(11) + 1.0

THETA = GAMMA - DELTA

PI = ALPHA**2/RS**2

PSI(1) = RETA/PI

HDOT = VP(1)*TP(1)*RA(1) **2

VBAR = ALPHA/RS**2

TBAR = HDOT/ (VBAR*RS**2)

WRITE OUTPUT TAPE 4 , 190

190 FORMAT (1H1)

WRITE DUTPUT TAPE 4,162

102 FORMAT (6X,31-X/D,7X,2HRA,8X,2HRP,8X,2HVP,8X,2HVS,8X,3HRAI,

```
PRINT 133, DIST(1), RA(1), RB(1), VP(1), VS(1), RAT(1), RBT(1),
17X, 3HRBI, 6X, 2HIP, 9X, 2HIS, 8X, 2HDP, 5X, 8HMOMENIUM//)
                                                                                 1TP(1), TS(1), CP(1), PSI(1)
                                                                                                                     104 RA(I + 1) = RA(I) - 0.1
                                                                                                                                                                                                   VS(I + 1) = VS(I)
                                                                                                                                                               VP(I + 1) = VP(I)
                                                                                                                                                                                                                                              I + I = I
```

107 TAU = VP(I)*RA(I)**2 + VS(I)*(RS**2 - RB(I)**2) OMEGA = VAVE*(RY**2 - RX**2) - 4.0*DV*CHI**2 IF (1.005*ALPHA - CMEGA - TAU) 109,110,110 0x(1) = 01ST(1) - 01ST(1 - 1)108 DV = (VP(I) - VS(I))/2.3VAVE = VS(I) + DVRX = RA(I)RY = RB(I)

DIST(1) = SQRTF((RB(1) - 1.0)/PARAB1)

106 CHI = (RB(I) - RA(I))/3, 1415926

199 IF (RS - RB(II)) 122, 122, 105

105 IF (RA(1)) 137,106,106

```
113 SIGMA = VAVE**2*(RY**2 - RX**2) - 8.0*VAVE*DV*CHI**2 +
109 VS(I) = VS(I) + (ALPHA - OMEGA - TAU)/(15.0*RB(I)**2)
                                                                                                                                                                                                                                                                                                                                                                              112 TAU = VP(I) **2*RA(I) **2 + VS(I) **2*(RS**2 - RB(I) **2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF (1.005*(GAMMA - P(I)) - VP(I)**2) 115,136,114
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             114 IF (0.995*(GAMMA - P(I)) - VP(I)**2) 136,136,116
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     1DV**2*CHI*RY*3.1415926 - 4.9348C22*CHI**2*DV**2
                                                                                                                                                                                                                                                                                                                                110 IF (0.995*ALPHA - CMEGA - TAU) 112,112,109
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DP(1) = (BETA - SIGMA - TAU)/(0.5*RS**2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          136 RB(I + 1) = 2.0*RB(I) - RB(I - 1)
                                                                                             192 VP(I) = SQRTF(VS(I)**2 + THETA)
                                                                                                                                                                                           LONG = ABSF(THETA - VS**2)
                                             IF (VS(I))193,192,192
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   P(1) = P(1) + OP(1)
                                                                                                                                                                                                                                      193 VP(I) = SORTF(LONG)
                                                                                                                                                                                                                                                                                                                                                                                                                            RY = RB(I)
                                                                                                                                           GO TO 107
                                                                                                                                                                                                                                                                                  GO TO 107
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            GO TO 132
```

```
115 RB(I) = RB(I) + 0.001
```

$$116 RB(I) = RB(I) - 0.001$$

$$RX = RA(1)$$

$$DX(I) = DX(I - 1)*(RA(I) - RA(I-1))/(RA(I-1) - RA(I-2))$$

$$DIST(1) = DIST(1-1) + Ox(1)$$

$$124 \text{ DV} = (\text{VP(I)} - \text{VS(I)})/2.0$$

$$TAU = VP(1)*RA(1)**2$$

$$VAVE = VS(1) + CV$$

$$CHI = (RS - RA(I))/3.1415926$$

```
128 TAU = VP(1) ** 2 * RA(1) ** 2
```

$$P(1) = P(1) + DP(1)$$

131 VP(1) = VP(1) - 0.0001

$$RAT(I) = RA(I) - 0.01*DIST(I)$$

$$300 \text{ TP}(1) = 1P(1)$$

$$93 TS(1) = TS(1)$$

```
ETA = VP(I) *IP(I) *RAT(I) **2+VP(I) *TAVE *(RA(I) **2-RAT(I) **2)+
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    12.0 % VP(I) *DT *CHIB * RA(I) * SINF(ANA) +2.0 * VP(I) * DT * CHIB * *2 *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                32.0*VS(1)*DT*CHIP*RB(1)*SINF(ANB)+2.0*VS(1)*CT*CHIB**2*
DB = (RB(I) - RA(I)) *3.1415926/(100.0*(RB(I) - RA(I)))
                                                                                                                                                                                                                                                                                                                                            ANB = (RB(I) - RAT(I)) *3.1415926/(RET(I) - RAT(I))
                                                                                                                                                                                                                              ANA = (RA(I) - RAT(I))*3.1415926/(RBT(I) - RAT(I))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SIG(J) = (VAVE+DV*COSF(ANC))*(TAVE+DT*COSF(ANA))*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2(COSF(ANA)-1.0)+VS(I)*TAVE*(RBT(I)**2-RB(I)**2)-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        4(1.0-COSF(ANB))+VS(I)*TS(I)*(RS**2-RBI(I)**2)
                                                                                                                                                                                                                                                                                         CHIB = (RBI(I) - RAT(I)) /3.1415926
                                                                                                                       RA(1) + 0.005*(RB(1) - RA(1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1((RZ+C.01*(38(I)-RA(I))) **2-RZ**2)
                                                                                                                                                                          CHIA = (RAT(I) - RA(I))/3.1415926
                                                                                                                                                                                                                                                                                                                                                                                                                                                          TAVE = 0.5*(TP(I) + TS(I))
                                                              0T = (TP(1) - TS(1))/2.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              DO 303 J = 1,100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ANA = ANA + DA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ANC = ANC + CB
```

RZ = RZ + 0.01 * (RP(1) - RA(1))

ZETA = ZETA + SIG(J)

303 CONTINUE

1F (1.005*HDCT - ETA - ZETA) 305,328,304

304 IF (0.995*HDE1 - ETA - ZETA) 328,328,305

305 RA1(1) = RAT(1) + (HDBT-EIA-ZETA)/(100.0*TP(1))

IF (RAT(I)) 170,302,302

170 RAT(1) = 0.0

GC TF 316

307 RRI(II) = RS

RAT(I) = RAT(I-1)**2/RAT(I-2)

IF (RAI(11)) 321,90,90

90 DA = (RS - RA(1)) x 3, 1415926/(100.0 x (RBI(1) - RAI(1))) - RA(1))*3.1415926/(100.0*(RE(1) - RA(1))) DR = (RS

15(1) = 15(1 - 1) **2/15(1 - 2)

308 OT = (TP(11) - 15(1))/2.0

83 LEIA = 0.0

RZ = RA(I) + 0.005 × (RR(I) - RA(I))

```
ETA = VP(1) *TP(1) *RAT(1) **2+VP(1) *TAVE * (RA(1) **2-RAT(1) **2) +
                                                                                                                                                                                                                                                                                                                                                                                                      12.0*VP(1)*DT*CHIB*RA(1)* SINF (ANA)+2.0*VP(I)*DT*CHIB**2*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   32.0*VS(I)*DT*CHIB*RB(I)*SINF(ANB)+2.0*VS(I)*DT*CHIB**2*
                                                                                                                                                                              RAT(1))
                                                       ANA = (RA(I) - RAT(I)) *3.1415926/(RBT(I) - RAT(I))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SIG(J) = (VAVE+DV*COSF(ANC))*(TAVE+DT*COSF(ANA))*
                                                                                                                                                                                                                                                                                                                                                                                                                                                             2(COSF(ANA)-1.0)+VS(I)*TAVE*(RBT(I)**2-RB(I)**2)-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           4(1.0-COSF(ANE))+VS(I)*TS(I)*(RS**2-RBT(I)**2)
                                                                                                                                                                    ANB = (RB(1) - RAT(1))*3.1415926/(RET(1) -
                                                                                                                 CHIB = (RBT(1) - RAT(1))/3.1415926
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1 ((RZ+0.01*(RB(I)-RA(I))) **2-RZ**2)
CHIA = (RAT(1) - RA(1))/3.1415926
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           RZ = RZ + 0.C1*(RB(I) - RA(I))
                                                                                                                                                                                                                                                                                    TAVE = 0.5*(TP(1) + TS(1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     00 309 3 = 1,100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ANC = ANC + DP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ANA = ANA + DA
```

ZETA = ZETA + SIG(J)

309 CONTINUE

IF (1.005*HDCT - ETA - ZETA) 311,328,310

310 IF (0.995*HDCT - ETA - ZETA) 328,328,311

311 TS(1) = TS(1) + (HOOT - ETA - ZETA)/(20.0*RS*#2)

GO TO 308

313 RBT(I) = 1.0 + PARAB2*DIST(I)**2

TP(I) = TP(I - 1) **2/TP(I - 2)

314 IF (RS - RBT(II)1 321, 321, 315

315 TS(1) = TS(1)

RAT(1) = 0.0

316 ZETA = 0.0

DA = (RB(I) - RA(I))*3.1415926/(100.0* RBT(I))

DB = (RB(I) - RA(I))*3.1415926/(100.0*(RB(I) - RA(I)))

DT = (TP(11) - TS(11))/2.0

RZ = RA(I) + 0.005*(RB(I.) - RA(I))

CHIA = (RAT(1) - RA(1))/3.1415926

ANA = (RA(I) - RAT(I)) +3.1415926/(RBT(I) - RAT(I))

CHIB = (RBI(I) - RAT(I)) /3.1415926

ANB = (RB(I) - RAT(I)) +3.1415926/(RBT(I) - RAT(I))

ANC = 0.0

TAVE = 0.5*(IP(1) + TS(1))

ETA = VP(I) *TP(I) *RAT(I) **2+VP(I) *TAVE *(RA(I) **2-RAT(I) **2)+

12.0*VP(I)*DT*CHIB*RA(I)*SINF(ANA)+2.0*VP(I)*DT*CHIB**2*

2(COSF(ANA)-1.0)+VS(I)*JAVE*(RBT(I)**2-RB(I)**2)-

32.0*VS(I)*DT*CHIB*RP(I)*SINF(ANB)+2.0*VS(I)*DT*CHIB**2*

4(1.0-COSF(ANB))+VS(I)*TS(I)*(RS**2-RBI(I)**2)

00 317 J = 1,100

SIG(J) = (VAVE+DV*COSF(ANC))*(TAVE+DT*COSF(ANA))*

1((RZ+0.01*(RB(I)-RA(I))) **2-RZ**2)

ANA = ANA + CA

ANC = ANC + CB

RZ = RZ + 0.C1*(RB(I) - RA(I))

ZETA = ZETA + SIG(J)

317 CONTINUE

IF (1.005 *HEOI - ETA - ZETA) 319,328,318

318 IF (0.995*HDCT - ETA - ZETA) 328,328,319

319 TP(I) = TP(I) +(HDOI - EIA - ZEIA)/((RA(I) + 0.5*(RBI(I)

1RAT(1)))**2 *VP(1)*5.0)

IF (TP(1) - TP(1)) 316,316,320

320 TP(1) = TP(1)

60 TO 302

321 RAT(1) = 0.0

RBT(1) = RSTS(1) = 2.0*1S(1 - 1) - TS(1 - 2)

DVP = VP(I) - V3AR

DA = (RB(I) - RA(I))*3.1415926/(100.0*RS)

DB = (RB(I) - RA(I))*3.1415926/(100.0*(RB(I) - RA(I)))

IF (FLAG) 322,322,378

322 STAR = (TP(I-1)-TBAR) *VBAR/((VP(I-1)-VBAR)*TBAR)

TP(1) = TBAR + STAR*DVP*TBAR/VBAR

CONST = (TP(I) - TBAR)*VBAR/((VP(I) - VBAR)*TBAR)

GO TO 323

378 TP(1) = TBAR + CONST*DVP *TBAR/VBAR

323 ZETA = 0.0

365 DT = (TP(1) - TS(1))/2.0

RZ = RA(I) + 0.005*(RB(I) - RA(I))

CHIA = (RAT(1) - RA(1))/3.1415926

ANA = (RA(I) - RAT(I))*3.1415926/(RBT(I) = RAT(I))

CHIB = (RBT(I) - RAT(I))/3.1415926

ANB = (RB(1) - RAT(1))*3.1415926/(RBT(1) - RAT(1))

ANC = 0.0

TAVE = 0.5*(TP(I) + TS(I))

ETA = VP(I) * TP(I) * RAT(I) * * 2 + VP(I) * TAVE * (RA(I) * * 2 - RAT(I) * * 2) +

12.0*VP(1)*DT*CHIB*RA(1)*SINF(ANA)+2.0*VP(1)*DT*CHIB**2*

2(COSF(ANA)-1.0)+VS(I)*TAVE*(RBT(I)**2-RB(I)**2)-

32.0*VS(1)*DT*CHIB*RB(1)*SINF(ANB)+2.0*VS(I)*DT*CHIB**2*

4(1.0-COSF(ANB))+VS(I)*TS(I)*(RS**2-RBI(I)**2)

00.324 J = 1,100

SIG(J) = (VAVE+DV*COSF(ANC))*(TAVE+DT*COSF(ANA))*

1((RZ+0.01*(RE(I)-RA(I)))**2-RZ**2)

ANA = ANA + CA

ANC = ANC + CB

RZ = RZ + 0.01*(RB(1) - RA(1))

ZETA = ZETA + SIG(J)

324 CONTINUE

IF (1.005*HDCT - ETA - ZETA) 326,366,325

25 IF (0.995*HDCT - ETA - ZETA) 366,366,326

326 TS(I) = TS(I) + (HDOF - ETA - ZETA)/(0.5*(VP(I) + VS(I))*RS**2) 60 10 323

366 FLAG = FLAG + 1.0

328 RB(I + 1) = 2.0*RB(I) - RB(I - 1)

PRINT 133, DIST(1), RA(1), RB(1), VP(1), VS(1), RAT(1), RBT(1),

11P(1), TS(1), OP(1), PS1(1)

133 FORMAT (11F10.4/)

GO TO 104

135 VP(1) = VP(1) + 0.0001

GO TO 124

137 TAU = VS(I)*(RS**2 - RB(I)**2)

RA(I) = 0.0

RX = 0.0

RY = RB(I)

CHI = RB(11/3,1415926

DIST(1) = SQRTF((RB(1) - 1.0)/PARAB1)

0x(1) = 01ST(1) - 01ST(1 - 1)

138 DV = (VP(I) - VS(I))/2.0

VAVE = VS(1) + DV

OMEGA = VAVE * (RY**2 - RX **2) - 4.0*DV*CHI**2

IF (1.005*ALPHA - OMEGA - TAU) 140,142,139

139 IF (0.995*ALPHA - OMEGA - TAU) 142,142,140

140 VP(1) = VP(1) + (ALPHA - OMEGA - TAU)/(10.0*RS**2)

. GO TO 138

142 TAU = VS(1)**2*(RS**2 - RB(1)**2)

SIGMA = VAVE**2*(RY**2 - RX**2) - 8.0*VAVE*DV*CHI**2 +

1DV**2*CHI*RY*3.1415926 - 4.9348022*CHI**2*DV**2

DP(1) = (BETA - SIGMA - TAU)/(0.5*RS**2)

P(1) = P(1) + OP(1)

50 IF (VS(I) - 0.2) 51,196,196

51 VEL = ABSF (CELTA - P(I))

IF (DELTA - P(I)) 52,53,53

52 VSB = -SQRTF(VEL)

60 10 54

53 VSB = SQRTF(VEL)

54 IF (VSB - VS(I) + 0.01)145,55,55

55 IF (VSB - VS(I) - 0.01)144,144,146

196 IF (1.005*(DELTA - P(I)) - VS(I)**2) 145,144,143

143 IF (0.995* (DELTA - P(I)) - VS(I) **2) 144,144,146

144 RB(I + 1) = RB(I) + 0.01

GO TO 132

145 VS(I) = VS(I) - 0.001

GO TO 137

146 VS(I) = VS(I) + 0.009

60 10 137

147 RA(I) = 0.0

RX = 0.0

RB(II) = RSRY = RS

TAU = 0.0

CHI = RS/3.1415926

VP(I) = VP(I - 1) - 2.0

148 DV = (VP(1) - VS(1))/2.0

VAVE = VS(I) + DV

OMEGA = VAVE * (RY**2 - RX**2) - 4.0*DV*CHI**2

IF (ALPHA - CMEGA + 0.001)150,149,149

149 IF (ALPHA - CMEGA - 0.001) 152,152,151

150 VS(1) = VS(1) - 0.00007

GO TO 148

151 VS(I) = VS(I) + 0.0001

GO TC 148

152 SIGMA = VAVE **2*(RY**2 - RX**2) - 8.0*VAVE *DV*CHI**2 +

1DV**2*CHI*RY*3.1415926 - 4.9348022*CHI**2*DV**2

DP(I) = (BETA - SIGMA - TAU)/(0.5*RS**2)

P(1) = P(1) + DP(1)

DX(I) = DP(I)*CP(I - 2)*DX(I - 1)**2/(DX(I - 2)*CP(I - 1)**2)

DIST(1) = DIST(1 - 1) + DX(1)

PSI(I) = (SIGMA + TAU)/PI

371 RAT(I) = 0.0

RBT(II) = RS

TS(I) = TS(I - 1) * *2/TS(I - 2)

DVP = VP(I) - VBAR

DA = (RB(1) - RA(1))*3.1415526/(100.0*RS)

DB = (RB(I) - RA(I))*3.1415926/(100.0*(RB(I) - RA(I)))

IF (FLAG) 372,372,379

72 STAR = (TP(I-1)-TBAR)*VBAR/((VP(I-1)-VBAR)*TBAR)

TP(1) = TBAR + STAR*DVP*TBAR/VBAR

CONST = (TP(I) - TBAR) *VBAR/((VP(I) - VBAR)*TBAR)

GO TO 373

379 TP(I) = TBAR + CONST*DVP*TBAR/VBAR

373 ZETA = 0.0

360 DT = (TP(I) - TS(I))/2.0

RZ = RA(I) + 0.005*(RB(I) - RA(I))

CHIA = (RAT(I) - RA(I))/3.1415926

ANA = (RA(I) - RAT(I))*3.1415926/(RBT(I) - RAT(I))

CHIB = (RBT(I) - RAT(I))/3.1415926

ANB = (RB(1) - RAT(1))*3.1415926/(RBT(1) - RAT(1))

VC = 0.0

TAVE = 0.5*(1P(1) + TS(1))

ETA = VP(1)*TP(1)*RAT(1) **2+VP(1)*TAVE*(RA(1) **2-RAT(1) **2)+

12.0*VP(I)*DT*CHIB*RA(I)*SINF(ANA)+2.0*VP(I)*DT*CHIB**2*

2(COSF(ANA)-1.0)+VS(I)*TAVE*(RBT(I)**2-RB(I)**2)-

32.0*VS(I)*DT*CHIB*RR(I)*SINF(ANB)+2.0*VS(I)*DT*CHIB**2*

4(1.0-COSF(ANB))+VS(I)*TS(I)*(RS**2-RBT(I)**2)

00374 J = 1,100

SIG(J) = (VAVE+DV*COSF(ANC))*(TAVE+CT*COSF(ANA))*

1((RZ+0.01*(RB(I)-RA(I))) **2-RZ**2)

ANA = ANA + CA

ANC = ANC + DB

RZ = RZ + 0.01*(RB(1) - RA(1))

ZETA = ZETA + SIG(J)

374 CONTINUE

IF (1.005*HDCT - ETA - ZETA) 376,350,375

375 IF (0.995*HDCT - ETA - ZETA) 350,350,376

376 TS(1) = TS(1) + (HDOT - ETA - ZETA)/(0.5*(VP(1) + VS(1))*RS**2)

60 10 373

350 FLAG = FLAG + 1.0

IF (VP(I) - VS(I)) 400,401,401

```
400 \text{ VP(I)} = \text{VAVE}
```

$$VS(I) = VAVE + 0.000000001$$

$$TP(1) = TAVE$$

$$TS(I) = TAVE$$

$$PSI(I) = 1.0$$

$$VS(I + 1) = VS(I) + 0.0001$$

VP(1 + 1) = VP(1) - 2.0

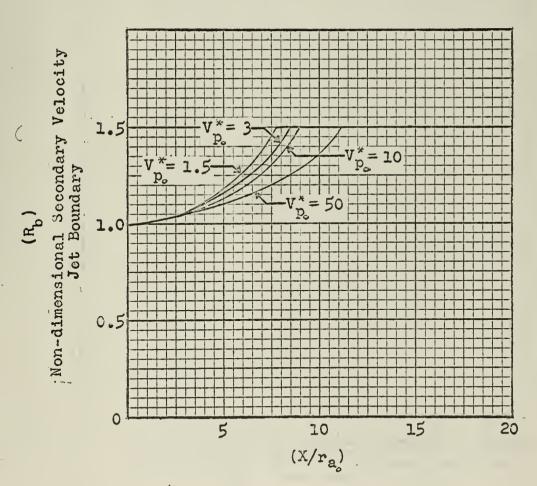
$$154 I = I + 1$$

END

APPENDIX II

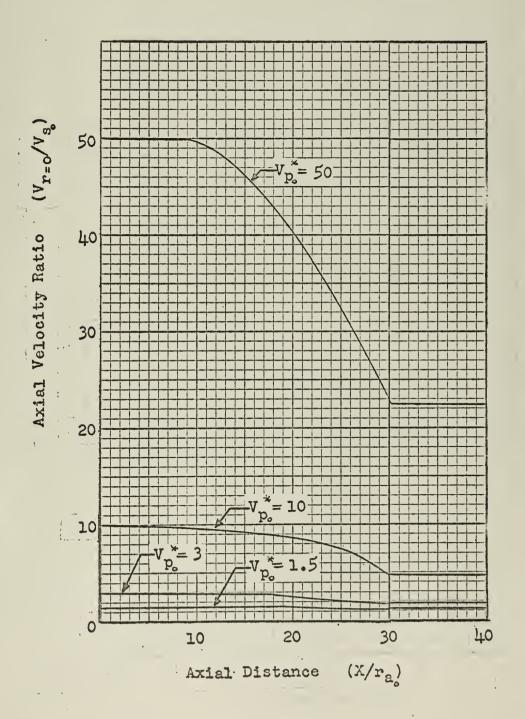
Appendix II is a graphical presentation of the data obtained by programs EJECTMIX I and EJECTMIX II. Various physical characteristics are plotted against the axial distance. The axial distance is expressed as a multiple of the central jet radius. The various curves shown represent data obtained using different initial central velocity ratios.

Non-dimensional Secondary Velocity Jet Boundary vs. Axial Distance for an Area Ratio of 2.25:1

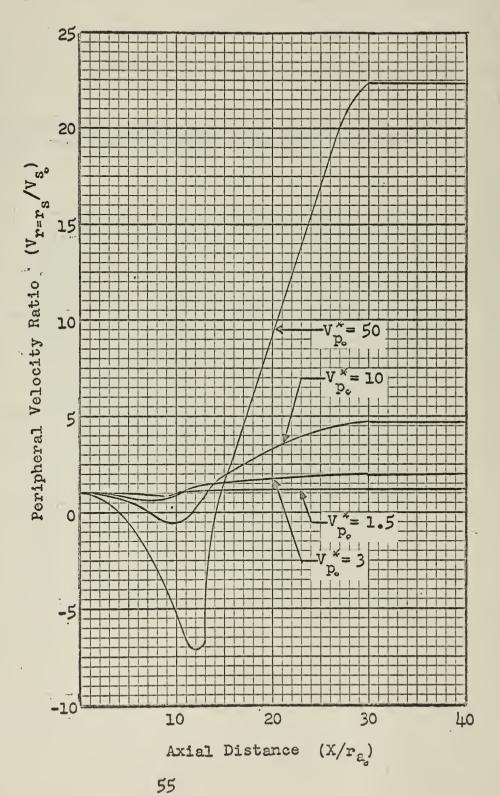


Axial Distance

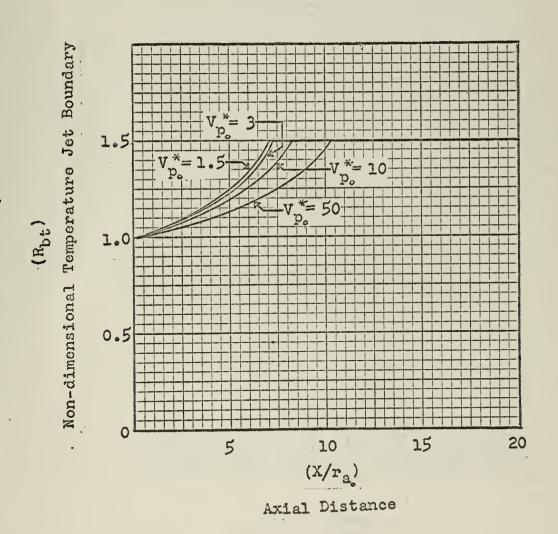
Axial Velocity Ratios vs. Axial Distance for an Ejector Area Ratio of 2.25:1

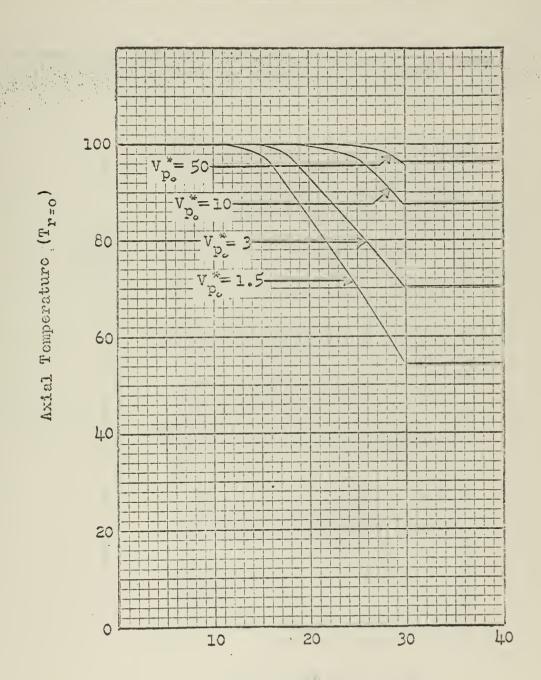


Peripheral Velocity Ratio vs. Axial Distance for an Ejector Area Ratio of 2.25:1



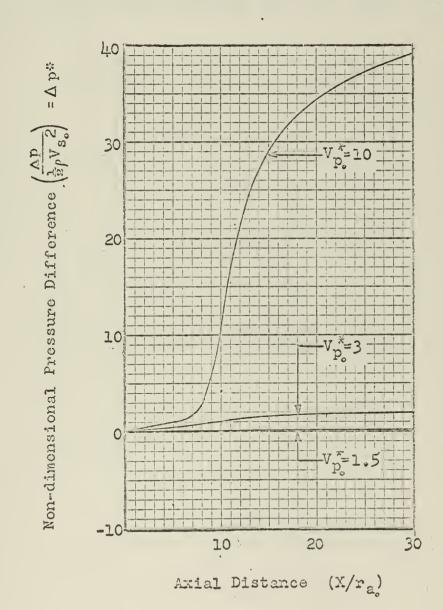
Non-dimensional Temperature Jet Boundary vs. Axial Distance for an Ejector Area Ratio of 2.25:1





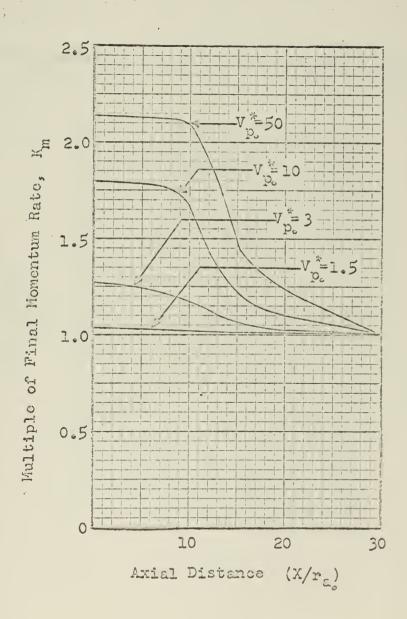
Axial Distance (X/ra)

Non-dimensional Pressure Difference vs. Axial Distance for an Ejector Area Ratio of 2.25:1

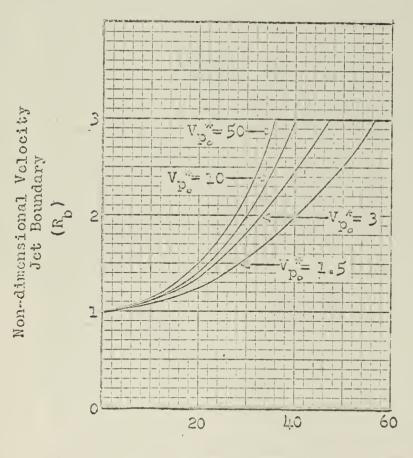


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Multiple of Final Momentum Rate vs. Axial Distance for an Ejector Area Ratio of 2.25:1

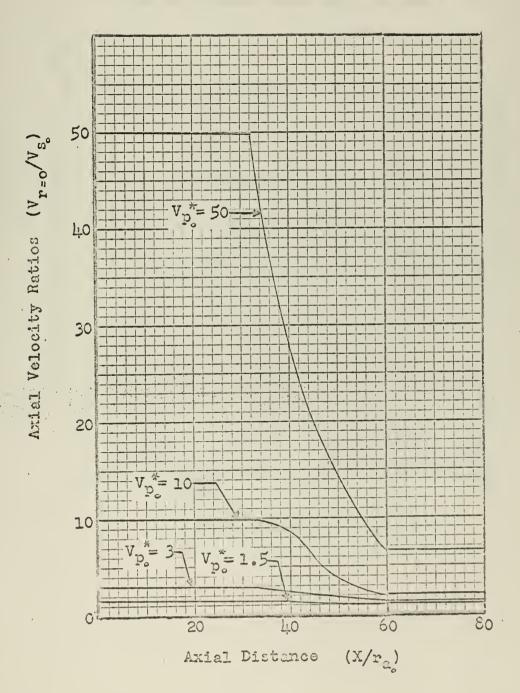


Non-dimensional Velocity Jet Boundary vs. Axial Distance for an Ejector Area Ratio of 9:1

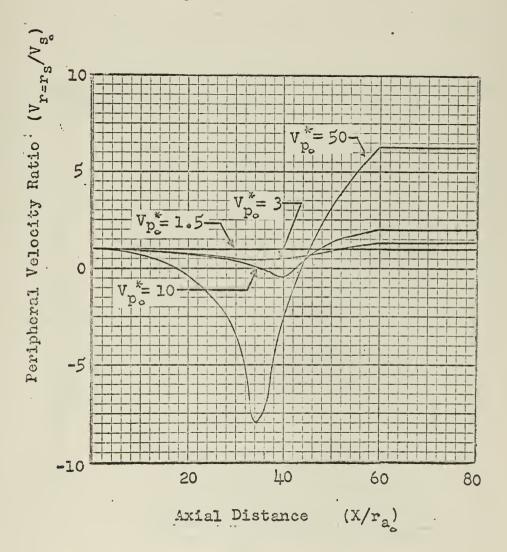


Axial Distance (X/ra)

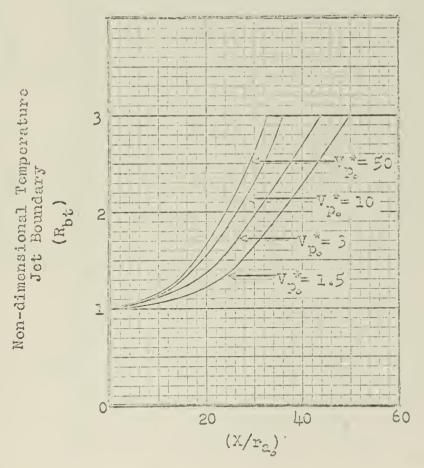
Axial Velocity Ratios vs. Axial Distance for an Ejector Area Ratio of 9:1



Peripheral Velocity Ratio vs. Axial Distance for an Ejector Area Ratio of 9:1

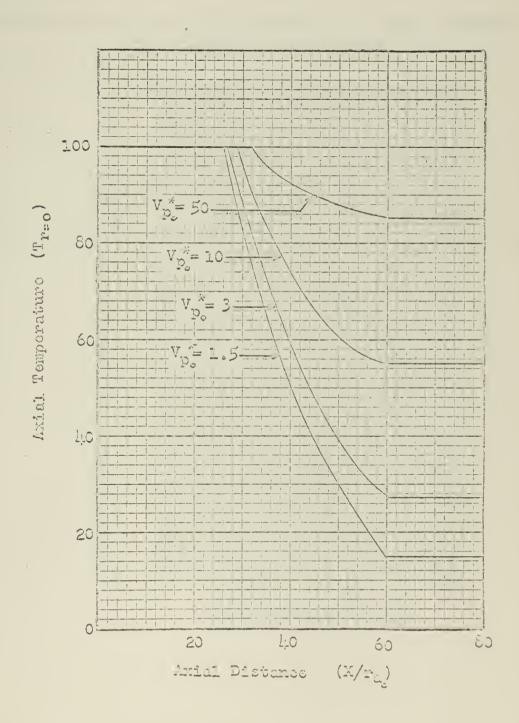


Won-dimensional Temperature Jet Boundary vs. Axial Distance for an Ejector Area Ratio of 9:1

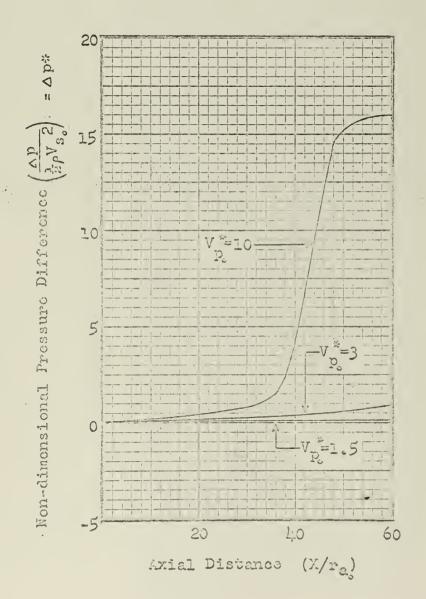


Axial Distance

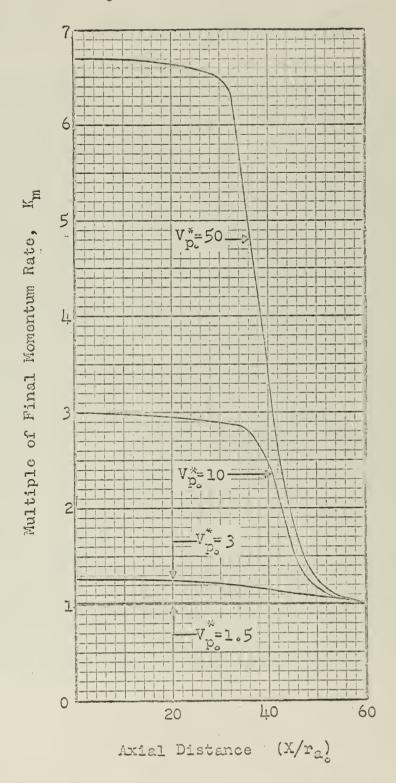
Axial Temperature vs. Axial Distance for an Ejector Area Ratio of 9:1



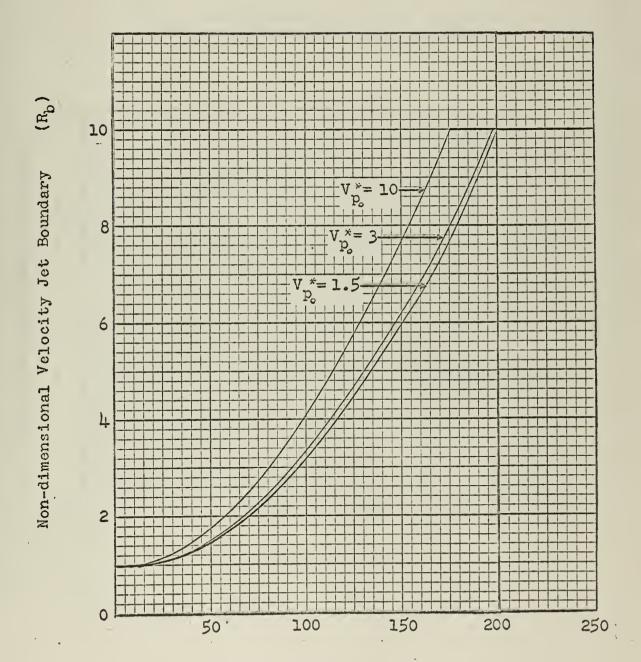
Non-dimensional Pressure Difference vs. Axial Distance for an Ejector Area Ratio of 9:1



Multiple of Final Momentum Rate vs. Axial Distance for an Ejector Area Ratio of 9:1

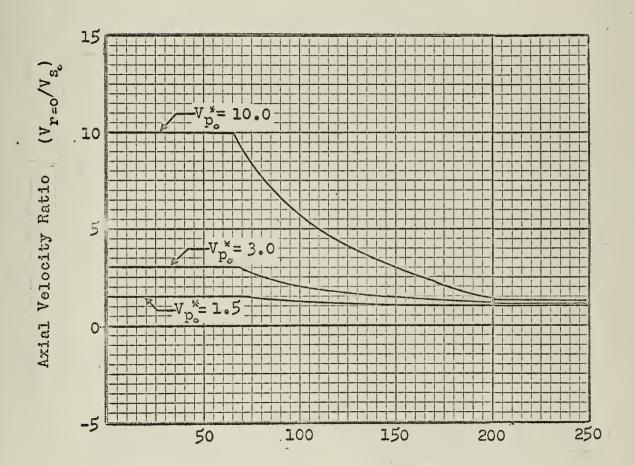


66



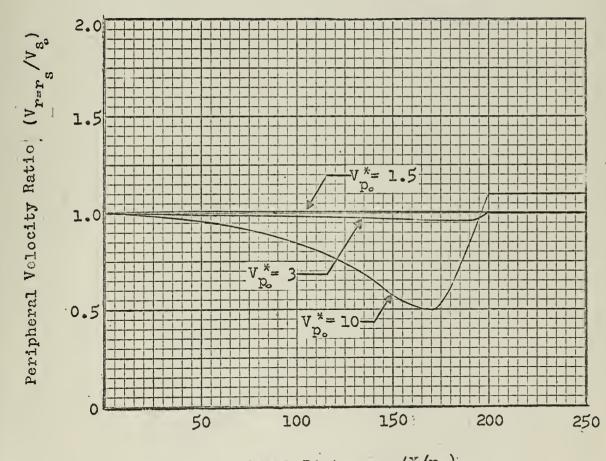
Axial Distance (X/r_a)

Axial Velocity Ratio vs. Axial Distance for an Ejector Area Ratio of 100:1

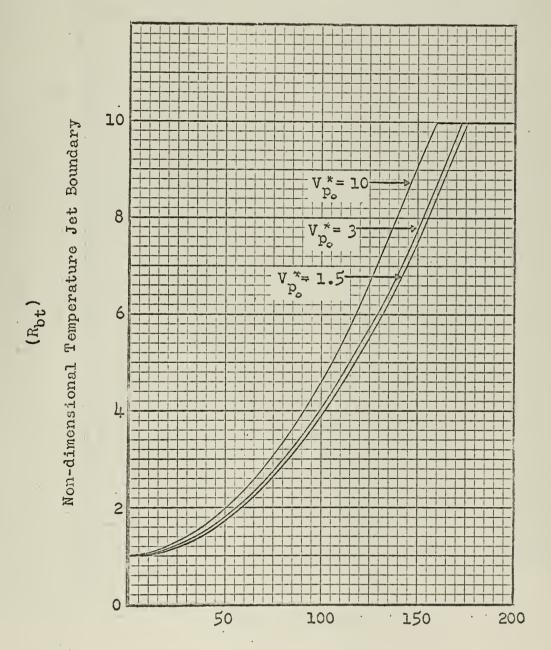


Axial Distance (X/ra)

Peripheral Velocity Ratio vs. Axial Distance for an Ejector Area Ratio of 100:1

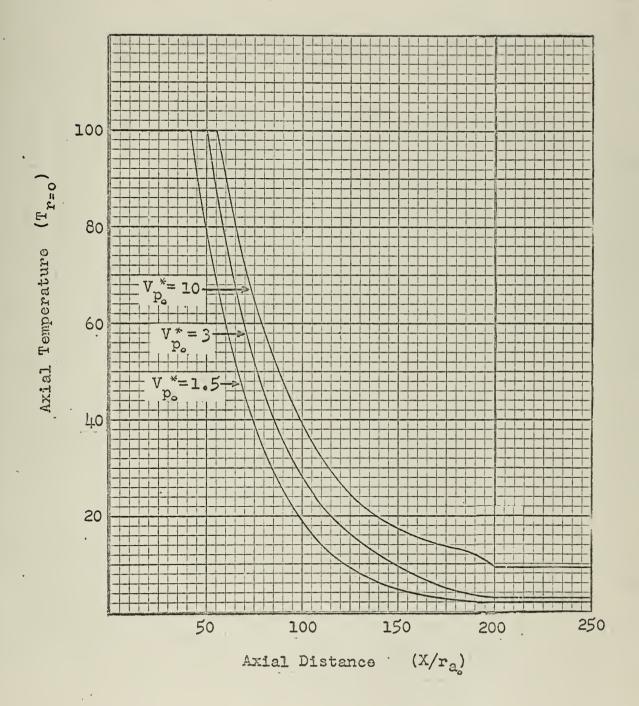


Axial Distance (X/ra)

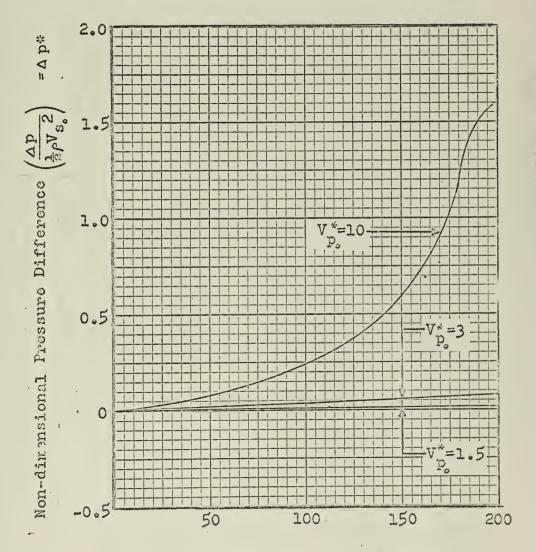


Axial Distance (X/r_a)

Axial Temperature vs. Axial Distance for an Ejector Area Ratio of 100:1.

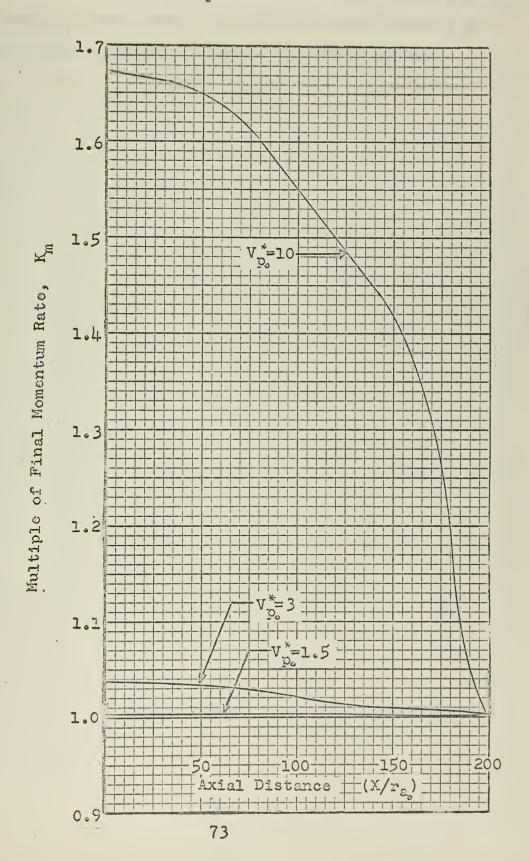


Non-dimensional Pressure Difference vs. Axial Distance for an Ejector Area Ratio of 100:1



Axial Distance (X/ra)

Multiple of Final Momentum Rate vs. Axial Distance for an Ejector Area Ratio of 100:1



APPENDIX III

Appendix III contains edited data from which the graphs of Appendix II were drawn. The headings are the same as defined in the section of Symbols and Abbreviations.

Central Velocity Ratio of 1.5 and Paipheral Radius Ratio of 1.5

of the same				,						
χ/r_{a_s}	RA	RR	٩٨	۸S	RAT	RBT	TP	TS	dQ	MOMENTUM
0.0	0.001.0000		1.5000	1.0000	1.0000	1.0000	.0000 1.5000 1.0000 1.0000 1.0000 100.0000	0000	.0000	1.0413
3.9	.90001	•	1075 1.4987	. 9980	.8596	1.1398	.8596 1.1398 100.0000	.0000	.0089	1.0384
5.6	.80001	•	22221.4950	.9925	9989.	1.2888	.6866 1.2888 100.0000	0000	.0199	1.0347
6.9	.70001		.3363 1.4905	.9857		1.4378	.4243 1.4378 100.0000	0000	.0311	1.0309
8.0	.60001	•	45141.4852	9226.	.2622	1.5000	.2622 1.5000 100.0000	3.1283	.0427	1.0270
9.1	.50001	•	5000 1.4837	.9938		1.5000	.1621 1.5000 100.0000	3.3169 .0593	.0593	1.0215
10.2	. 40001	•	50001.47891.0306	1.0306		1.5000	.1002 1.5000 100.0000	4.6390	.0738	1.0166
11.3	.30001	•	5000 1.4750 1.0597	1.0597	.0619	1.5000	.06191.5000100.0000	5.8913	6480.	1.0129
15.0	.20001	•	5000 1.4721 1.0830	1.0830	00000	.0000 1.5000	4784.66	7.1436	.0933	1.0101
18.5	.10001	•	5000 1.4700 1.1019	1.1019	00000	.0000 1.5000	99.1098	7.2033	8660.	1.0079
22.5	.00001	•	5000 1.3700 1.1591	1.1591	0000	.0000 1.5000	81.1250 25.4019 .1181	25.4019	.1181	1.0018
26.1	.0000		50001.27001.2015	1.2015		.0000 1.5000	63.1402 45.0112 .1245	45.0112	.1245	9666.
30.0	.0000	•	50001.17001.2437	1.2437		.0000 1.5000	45.1555 63.5511 .1247	63.5511	.1247	9666.

1.5	MOMENTUM	1.2768	1.2589	1.2383	1.2135	1.1582	1.1132	1.0844	1.0645	1.0500	1.0391	1.0243	1.0179	1.0125	1.0080	1.0045	1.0019	1.0003	9666.	. 9998
Ratio of	фQ	0000*	.1278	.2747	.4516	·8466	1.1676	1.3732	1.5154	1.6187	1.6963	1.8017	1.8474	1.8863	1.9184	1.9432	1.96.1	1.9735	1.9784	1.9765
ns of Radius Rat	1.5	0000*	• 0000	• 0000	10.9593	17.3726	26.2395	30.3976	32.7374	37.4182	38.8691	95.4042 41.4353	91.9590 45.3568	1619.61	54.0148	58.1286	61.5346	65.1401	68.9570	72.5203
0	1.0	100.0000	100.0000	100.000	100.0000	100.0000	100.0000	100.0000	100.0000	99.3454	86.8493	95.4042	91.9590	88.5139	85.0688	81.6236	78.1785	74.7334	71.2882	67.8431
Per	RBT	.0000	1.1902	1.3839	.5000	1.5000	1.5000	.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000
or Initial	RAT	1.00001	.8470	.6785	.54351	.4354	.3487	.2794	.2238	.0000	• 0000	10000	.0000	• 0000	.0000	.0000	10000	0000	.0000	. 0000
ata fo o of 3	VS	1.0000	.9361	.8537	.7423	.8866	1.0898	1.2338	1.3417	1.4255	1.4921	1.5835	1.6258	1.6681	1.7104	1.7528	1.7951	1.8374	1.8797	1.9220
Edited Data for ity Ratio of 3.	۷Þ	3.0000	2.9793	2.9545	2.9242	5000 2.8625	5000 2.80561	.50002.7685	2.74261	.5000 2.72361	2.7092	50002.6092	.50002.5092	.5000 2.4092	2.3092	2.20921	2.1092	50002.0092	1.9092	1.8092
Edi Velocity	RB	1.0000 3.00001.0000	1.1463	1.2953	1.4505	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	-	1.5000	1.5000
Central	RA	0.001.0000	0006.	.8000	.7000	. 6000	. 5000	0004.	.3000	. 2000	. 1000	00000	00000	0000	0000	0000	0000	0000	00000	00000
Ce	X/ra	0.0	4.6	6.5	8.1	9.7	10.8	12,8	14.3	15.8	17.4	19.0	80.5	22.0	23.5	24.9	26.2	27.5	28.7	30.0

Edited Data for Initial Conditions of Central Velocity Ratio of 10.0 and Peripheral Radius Ratio of 1.5

MORENTUM	1.8000	1.7786	1.7705	1.5934	1.3258	1.2132	1.1485	1.1063	1.0767	.0551	1.0059	1.0000
MOM										_		
00	0000	1.0681	1.4735	10.3283	23.7104	29.3393	32.5725	34.6869	36.1660	37.2453	39.7071	87. 8288 39. 6281
TS	0000	0000	0000	42.3383	60.1028 23.7104	70.7816	73.1986 32.5725	76.1276 34.6869	77.5881 36.1660	77.5988	82.5090 39.7071	ARCA TA
ТР	0.0 1.0000 1.0000 10.0000 1.0000 1.0000 1.0000 100.0000	100.0000	100.000	.5895 1.5000 100.0000 42.3383 10.3283	100.000	.4056 1.5000 100.0000 70.7816 29.3393	.3365 1.5000 100.0000	99.5527	59.2354	99.0016	52.1258	87 8288
RBT	1.0000	.8566 1.2028	.7106 1.4355	1.5000	.4890 1.5000	1.5000	1.5000	00001.5000	.0000 1.5000	1.5000	.00001.5000	20001 5000
RAT	1.0000							•		.0000		
۸S	1.0000	.6213	9.94871512	9.49316303	8.7561 1.0354	8.4268 1.9226	8.2319 2.5090	8.1018 2.9326	8.0095 3.2540	7.9415 3.5053	5.9415 4.6009	1, 4011
VP	10.0000	9.9693	9.9487		8.7561		8.2319		8.0095	7.9415		1, 401,11, 11, 4011,11
RB	1.0000	.9000 1.1560	8000 1.3350	1.5000	. 6000 1. 5000	1.5000	1.5000	1.5000	.2000 1.5000	1.5000	1.5000	0000
RA	1.0000		.8000	-7000 1.5		.50001.5	.40001.5	.3000 1.5		.10001.5	.0000	
X/ra	0.0	2.3	7.7	10.2	12.7	15.1.	17.6	20.1	22.6	25.1	27.6	30 0

Edited Data for Initial Conditions of Central Velocity Ratio of 50.0 and Peripheral Radius Ratio of 1.5

2															42			
MORENTUR	2.1427	2.1281	2.1012	1.8182	1.4133	1.2653	1.1838	1.1316	1.0955	1.0694	1.0523	1.0371	1.0244	1.0144	1.0070	1.0023	1.0001	1.0000
06	0000	15.0757	43.0149	336.7149	756.8047	910.3820	995.0087	1049.0897	1086.6187	1113.6232	1131.3694	1147.2041	1160.3187	1170.7131	1178.3873	1183.3412	1185.5750	1185.0886
TS	0000	0000	0000	72.2358	85.4229	94.1778	94.9378	95.1514	6836 • 46	1999.46	93.0335	92.0432	92.6695	93.3000	93.9347	94.5739	95.2173	96.6109
16	100.0000	1000000	100.0000	100.0000	100.0000	1000000	100.0000	59.8937	99.8188	99.7642	99.4633	59.1623	98.8614	98.5604	98.2595	97.9585	97.6576	96.6109
RBT	1.0000	1.2093	1.4420	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000
RAT	1.0000	.8618	.7583	. 6673	.5871	.5166	94540	0000	0000	0000	0000	0000	00000	0000	00000	0000	0000	0000
٧S	1.0000	-1.4517	-5.5528	-7.1640	2.5901	7.2986	10.3271	12.4847	14.1063	15.3703	17.4271	18.2735	19.1199	19.9663	20.8127	21.6591	22.5055	22.3858
VP	50.0000	49.9689	49.6806	46.7428	41.9593	40.0679	38.9865	38.2799	37.7825	37.4198	35.4198	33.4198	31.4198	29.4198	27.4198	25.4198	23.4198	22.3858
RB	1.0000	1.1610	1.3400	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	1.5000	0 1.5000	1.5000
RA	1.0000	0006.	.8000	.7000	0009.	.5000	0004.	.3000	.2000	.1000	00000	00000	0000	.0000	0000	.0000	00000	0000
X/rg	0.0	6.7	9.8	12.8	15.8	19.0	22.0	22.8		24.5	25.0	25.8	26.5	27.3	27.9	28.5	29.3	30.0

Edited Data for Initial Conditions of Central Velocity Ratio of 1.5 and Peripheral Radius Ratio of 3.0

MOMENTUM	1.0222	1.0209	1.0199	1.0191	1.0183	1.0175	1.0168	1.0162	1.0150	1.0142	1.0121	1.0095	1.0080	1.0068	1.0062	1.0056	1.0051	1.0046	1.0008	6666.
0.0	0000	.0028	6 4000	6900.	.0087	.0104	.0119	.0132	.0159	.0177	.0224	.0282	.0315	.0343	.0356	.0368	.0380	.0391	.0475	7640.
TS	0000	0000	. 0000	• 0000	.0000	.0000	.0000	0000	.0000	00000	0000	.0000	0000	9666.	2.0774	3.1552	4.1525	5.0281	10.7704	16.7642
TP	000.000	0000.000	0000.000	0000.000	0000.000	85.8086	73.7677	64.1954	57.1810	52.1133	43.9363	37.6743	32.5584	29.3300	28.3535	27.4540	26.6255	25.8623	20.2438 10.7704	14.6254 16.7642
RBT	1.0000	1.1063	1.2525	1.3988	1.5450	1.6913	1.8375	1.9838	.00002.1038	2.2145	.0000 2.4360	.00002.6576	2.8791	3.0000	.0000 3.0000	3.0000	.0000 3.0000	.0000 3.0000	3.0000	.00003.0000
RAT	1.00001.0000	.8997	.7238	.4992	7490.	00000	0000	• 0000		.0000			0000	.0000		.0000		. 0000	.00003	
VS		1.00.1	1.0000	.9987	1766.	.9953	.9933	6066.	.9895	.9886	.9886	. 9882	.9865	.9850	4486.	. 9838	.9832	.9826	1.0219	1.0348 1.0642
Λρ	1.5000	1.5007	1.5000	1.4991	1.4981	1.4969	1.4955	1.4940	1.4930	1.4924	1.4467	1.3816	1.3354	1.2966	1.2792	1.2632	1.2484	1.2348	1.1348	
RB	1.0003	1.0813	1.1943	1.3063	1.4193	1.5313	1.6443	1.7563	1.8491	1.9343	2.1047	2.2751	2.4455	2.6159	2.7011	2.7863	2.8715	2.9567	3.0000	3.0000
RA	1.0000	0006 •	.8000	.7000	. 6000	.5000	0004.	.3000	.2000	.1000	.0000	0000	.0000	00000	00000	00000	00000	00000	00000	.0000
X/ra	0.0	11.7	18.1	22.6	26.4	29.8	32.8	35.4	37.7	39.6	43.0	1.94	149.5	52.0	53.2	54.6	55.9	57.2	58.5	0.09

Edited Data for Initial Conditions of

	Central Velo	Velocity Re	Hatio of	3.0	and Fer	Feripheral	Radius Ka	Ratio of	3.0
RB		۸۷	٧S	RAT	RBT	ТР	15	DP	PCPENTUM
0.0 1.0000 1.0000	0	3.0000	0000.	1.0000	1.000	100.0000	0000	2000:	1.2645
. 90CC 1.1342	N	2.9971	.9912	. 8726	1.1534	100.000	0000.	.0224	1.2570
80CC 1.2686	2	2.9936	.9807	.7381	1.3070	100.000	0000	.0429	1.2501
.70C0 1.4C30	0	2.9897	.9688	.5651	1.4606	100.000	0000	.0612	1.2440
.60CC 1.5330	0	2.9857	4956	.3659	1.6091	100.000	0000	6080	1.2374
5000 1.6547	~	2.9822	.9451	.1222	1.7482	100,000	0000.	:1023	1.2302
.40CC 1.7727	~	2.9786	.9337	0000	1.8831	93.7517	0000-	.1239	1.2230
30CC 1.8870	0	2.975c	.9222	0000.	2.0137	85.0029	0000	.1453	1.2158
.20CC 1.9978	8	2.9714	. 9106	0000	2.1403	77.7631	0000	.1667	1.2087
.1000 2.1050	0	2.9678	. 8989	0000.	2.2629	71.1400	0000	.1879	1.2016
00CC 2.2122	()	2.9527	.8883	.0000	2.3854	66.0368	0000.	.2146	1.1926
.0000 2. 4266	10	2.7282	.8583	2000.	2.6304	57.8561	0000	.2667	1.1752
00CC 2.6410	0	2.5402	. 8274	0000.	2.8754	51.4610	0000	.3185	1.1579
.0000 2.8554		2.3800	. 7952	2222.	3.0000	47.3503	2.0831	.3707	1.1404
.0000 3.000c	0	2.2087	9408.	0000.	3.0000	44.3797	6.9525	9654.	1.1106
0000 3.000	0	2.0087	.8893	2222.	3.0000	40.5114	11.3241	.58cc	1.6703
cocc 3.00c0	0	1.8087	.9739	0000.	3.0000	37.4430	15.6057	.6735	1.0390
.0000 3.0000	0	1.6087	1.0585	2222.	3.0000	33.9747	19.6394.	.7358	1.0168
0000 3.0000	0	1.4087	1.1432	2000.	3.0000	30.5064	23.4311	.7786	1.0039
.0000 3. c000	0	1.2057	1.2273	2222.	3.0000	27.0381	27.1824	.7905	6666.
					1				Annual Co.

Central Velocity Ratio of 10.0 and Peripheral Radius Ratio of 3.0

							-													
MCM ENTUM	3.0000	2.5345	2.5173	2.5052	2.8575	2.8961	2.8573	2.5028	2.9102	2.5185	2.8015	2.5358	2.2445	1.5838	1.6838	1.3853	1.1719	1. 6434	1.0110	1.0003
00	.0000	.5210	.6616	.7584	.8199	.8312	.8215	1777.	.7185	.6523	1.5881	3.7139	6.0443	8.1255	10.5297	12.9174	14.6252	15.6529	15.9117	15.9980
TS INTERIOR	2000	0000-	0000	0000-	0000	2000 -	0000 •	0000.	0000 •	0000	16.7436	22.7348	27.0294	31.0321	36.0124	41.4602	46.0044	5C.2466	52.5122	55.0647
REI TP	1000000	10000001	100.000	100.000	10000001	10000001	10000001	8585.45	67.9086	82.0368	75.4231	73.620c	71.8169	70.0138	67.6057	64.6045	61.5993	58.5942	57.0916	55.2885
RET	1.0000	1.1612	1.3588	1.5564	1.7540	1.9516	2.1492	2.3468	2.5444	2.7420	3.000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000
RAT	1.0000	.5053	-7556	.6018	.4257	.2564	. 0672	2000.	2222.	2222 •	2222.	0000.	2222.	2222.	00000	0000	00000	2222.	2223.	2000.
S	1.0000	1616.	.9115	.8329	.7425	9449.	.5327	.4109	.2755	.1254	6766	0445	2901	0362	.3024	.7256	1.1488	1.5720	1.7836	2.0375
VP VP	0000°	9.9580	9.9915	2.9847	9.9775	9.9707	1 496.6	S. 9584	9.9537	5.9507	8.6111	8.0111	7.4111	6.8111	6.0111	5.0111	4.0111	3.0111	2.5111	1.9111
RE	1.00001	1.1240	1.2760	1.4280	1.5800	1.7320	1.8840	2.0360	2.1880	2.3400	2.9480	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000	3.0000
RA	1.0000	0006.	.8000	-7000	.6000	• 50cc	2224.	.3000	.20cc	.1000	0000-	00000	0000	0000.	.0000	.0000	00000	0000.	00000	2000.
X/ra	0.0	10.8	16.1	20.1	23.5	26.3	28.9	31.3	32.0	34.8	39.0	40.0	40.8	4.5	43.0	45.5	48.5	51.2	55.0	0.09

Edited Data for Initial Conditions of Central Velocity Ratio of 50.0 and Peripheral Radius Ratio of 3.0

PCP ENTUP	6.7059	6.6931	0.6770	6.6316	4.6287	4565.9	6.5457	6.5582	6.5529	0804.9	5.6015	435.	3.2852	2.5609	1.7490	1.4536	1.2319	1. 0839	1.0261	1.0000
00	2000-	1.3962	2.7308	6.4985	6.7445	9.6760	11.9769	12.5551	13.0355	25.0724	92.0672	195.6232	284.4612	344.6214	412.0555	436.5539	455.01C2	467.3061	472.1631	474.2740
15	0000	2022.	0000	0000	0000	0000.	0000	0000	0000.	0000	47.C827	55.7897	63.5951	68.0910	73.6293	76.1109	79.6422	80.8150	82.2272	84.1897
RET TP TS	1.0000100.0000	.1725 100.0000	100.000	1.5889 100.0000	1.7969 1CO. ECOO	· cc49 1c0.c000	2.2129 100.0000	100.000	.6081 ICC.CC00	2.7849 100.0000	87.0369	55.4541	53.8390	92.6146	4972.02	89.6673	88.6383	87.6692	87.0231	86.2156
			1.3809			2		2.4209	2		3.0000	3.000	3.0000	3.000	3.0000	3.0000	3.0000	3.000	3.0000	3.0000
RAT	0000-1	.9025	.7643	.6228	.4813	.3429	.2154	.1162	.0532	. 0158	2223.	2000	2000	0000.	2222.	2222.	0000.	• 6000	2000.	0000.
	1.00001	.8147	.3752	1313	9469	-1.3275	-2.0274	-2.8036	-3.5685	-4.2372	-7.7442	-5.6706	-3.5546	-1.8194	.7158	1.9893	3.2589	4.5285	5.3749	6.4329
RA RB VP VS	50.0000	49.9966	49.9914	49.9858	49.9852	49.9724	49.9489	49.9113	49.8625	49.8101	39.9713	35.0713	30.0713	25.9713	19.9713	16.9713	13.9713	10.9713	8.9713	6.4713
RB	1.0000	1.1330	8000 1.2930	70CC 1.4530	.60CC 1.6130	5000 1.7730	.40CC 1.9330	3000 2.0930	.20cc 2.2370	.10002.3730	. cocc 3.0000	3.0000	3.0000	3.0000	. COCC 3.0000	.0000 3.0000	. COCO 3.0000	3.0000	3.0000	3.0000
RA	0.01.00001.0000	.9000	•	•	_	•		•				• 0000	.0000	0000			00000	.0000	0000	0000
X/ra	0.0	6.6	14.8	18.3	21.4	24.0	26.4	28.5	30.2	32.0	34.7	36.3	38.5	0.14	45.0	47.9	50.14	53.5	56.0	0.09

MOMENTOM .0010 .0001 .0025 .0022 .0018 .0013 .0012 .0008 90000 .0005 4000° .0003 .0002 .0002 .0001 .0001 10.0 0000. .0005 .0033 .0014 .0025 .0029 .0024 9400. · 0047 .0037 00000 .0041 .0043 .0045 2400. .0048 1.5 and Peripheral Radius Ratio of OP .0000 .0000 0000 0000 0000. 2000. .0000 00000 0000 2000. 2000. 0000. 00000 00000 2000. 2000. TS of 65.2692 32.7236 8.0189 4.0688 23.9360 1.0000 100.0000 1.0390 100.0000 84.7126 47.2055 18.2645 Edited Data for Initial Conditions 100.0000 100.0000 13.6111 0.5225 6.3177 5.0981 T P 1.1170 6.7788 7.5557 8.4621 1.4701 1.7291 2.3765 2.8944 3.4123 3.9303 4.5777 6.0019 1.9881 5.2251 RBT .4222 .9442 0000 0000-2222. .5000|1.0000|1.0000| 9880 0000 2222. 0000 00000 0000 2222. 0000 2222. 0000 RAT 3.7521 1.11281.0003 .4450 1.0009 2.4573 1.2462 1.0006 .18851.0004 1.0000 2.0583 1.3387 1.0007 1.149811.0003 4.8477 1.0697 1.0001 1.0000 .5002 1.0003 .500611.0010 .5009 1.0013 .5007 1.0010 .0001 1.09061.0001 Central Velocity Ratio of < > < 1.05521 6.0429 1.0461 6.7401 1.0371 ۷P 1.0000.1 1.7601 1.03001 1.09001 1.5603 1.3617 5.4453 2.8557 4.2501 3.2541 RB .1000 • 0000 0000 2202. .0000 .7000 .3000 0000 2222. 0000-00000 0.0 1.0000 .9000 .0000 .0000 .0000 RA 80.5 110.8 149.8 68.6 140.9 11.6 58.1 160.0 120.2 130.8 100.0

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2.5074

10.0000

10.0000

00000

8.2341 1.0248 1.0000 9.1305 1.0202 1.0000

7.5369 1.0296 1.0000

170.8

179.5

Edited Data for Initial Conditions of

MCMENTUM	1.6381	1.0359	1.0351	1.0345	1.0336	1.0334	1.0324	1.0260	1.0232	1.0207	1.0178	1.0155	1.0130	1.0113	1.0092	1.0075	1.0061	1.0047	1.0036	1.0002
- 00.	0000	.0045	.0061	.0075	\$600.	.0098	.0118	.0250	.0309	.0362	.0421	.0470	.0521	.0558	.0600	.0635	.0665	.0695	.0718	.0789
TS	0000.	0000	0000	0000	2000.	2222.	2222.	2222.	0000	2222	2222.	0000	2222.	2222.	0000.	2222.	0000	.3924	.9263	2.4870
1P	100.000	100.0000	100.000	100.000	98.3064	74.5285	60.4734	46.0103	35.2190	28.0867	21.8323	17.4372	13.7198	11.4663	9.1290	7.4293	6.1664	5.2914	4.8347	3.3052
RET	1.0000	1.1144	1.2874	1.4605	1.8065	2.1526	2.4456	2.9713	3.4970	4.0228	4.6799	5.3371	6.1256	6.7828	7.7028	8.6228	9.5428	10.000	10.0000	10.000
RAT	0000	.928C	.7641	.5669	2222.	0000	2222	.0000	0000.	0000-	2200.	.0000	0000	.0000	2222.	2000.	2222.	0000-	0000.	0000.
VS	1.0000	1.0002	п666.	. 9985	. 9963	. 9937	.9916	.9898	.9867	.9840	.9811	. 9785	.9759	.9741	.9718	.9700	. 9685	6996.	.9657	1.0072
VP	3.0000	3.0001	2.9998	2.9995	2.9988	2.9979	2.9972	2.5923	2.2984	2.0781	1.8721	1.7203	1.5826	1.4939	1.3593	1.3268	1.2705	1.2151	1.1772	1.0502
RB	1.0000	1.0880	1.2211	1.3542	1.6204	1.8866	2.1120	2.5164	2.9208	3,3252	3.8307	4.3362	4.9428	5.4483	6.1560	6.8637	7.5714	8.4813	9.2901	10.0000
RA	1.0000	0006.	.8000	.7000	.5000	.3000	.1000	0000.	00000	2202.	00000	2202.	00000	2000.	0000.	2202	00000	0000	0000.	2222.
X/ra	0.0	19.6	31.0	39.3	52.0	62.1	69.7	81.3	91.3	10001	110.0	120.3	131.3	139.7	150.0	160.2	170.0	181.2	190.1	200.0

Edited Data for Initial Conditions of Central Velocity Ratio of 10.0 and Peripheral Radius ratio of 10.0

0.0	MOMENTUM	1.6749	1.6687	1.6651	1.6628	1.6533	1.6393	1.6221	1.6007	1.5803	1.5509	1.5323	1.5053	1.4790	1.4494	1.4202	1.3873	1.3540	1.1858	1.0416	1.0002
OT IO O	DP	0000	.0148	.0233	.0287	.0513	.0848	.1257	.1763	.2249	2948	.3388	.4030	.4656	.5359	.6052	.6835	.7626	1.1624	1.5049	1.6033
s ratio	15	0000	0000	0000	0000.	.0000	00000	0000.	00000	00000	0000	00000	00000	00000	0000	0000	.0331	1.8733	4.50931	7.0506	8.93061
ral nadius	ТР	100.0000	100.0000	100.0000	.100.0000	100.0000	88.3180	71.6688	57.5169	47.6419	37.4954	32.6706	27.2208	23.2470	19.8283	17.2912	15.2695	14.4701	12.8481	10.9134	9.3012
randt ra r	RBT	1.0000	1.1823	1.3646	1.5436	1.8731	2.3266	2.7489	3.3119	3.8750	4.7195	5.2826	6.1271	6.9717	7.9570	8.9423	10.0000	10.0000	10.0000	10.0000	10.0000
o alla	RAT	0000-1	8698	.7347	.5798	.2687	00000	00000	00000	0000	00000	00000	00000	.0000	00000	0000	0000	0000	.0000	.0000	0000.
70	٧S	1.0000	.9950	.9892	.9831	9716	.9543	.9363	.9089	.8818	.8415	.8146	.7740	.7327	.6827	.6299	.5639	· 4884	.6078	.8618	1.0733
JIGOTO	· VP	10.0000	6.9995	6866.6	9.9983	9.9972	9.9955	9964.6	8.0202	0.9540	5.8142	5.2518	4.5968	4.0970	3.6472	3.2958	2.9803	2.7324	2.2293	1.6293	1.1293
SO TOOTO	RB	1.0000	1.1513	1.3033	1.4533	1.7275	2.1055	2.4574	2.9265	3,3953	4.0995	4.5683	5.2725	1926.5	6.7975	7.6185	8.5570	4964.6	10.000	10.000	10.0000
י יייייייייייייייייייייייייייייייייייי	RA	1.0000	0006	.8000	. 7000	.5000	. 2000	0000	0000	00000	00000	00000	0000	0000	.0000	0000	0000	0000	00000	00000	0000
	X/ra	0.0	22.6	32.0	39.0	49.64	61.2	70.0	80.9	0.06	102.2	109.9	120.2	130.0	140.0	150.0	160.0	170.0	180.0	190.2	200.0

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